

Intuitionistic fuzzy Conjunctions and Disjunctions from Second Type

Nora Angelova¹, Miroslav Stoenchev², Venelin Todorov^{3,4}

Faculty of Mathematics and Informatics, Sofia University

E-mail: nora.angelova@fmi.uni-sofia.bg

² Dept. of Bioinformatics and Mathematical Modelling, Institute
of Biophysics and Biomedical Engineering, Bulgarian Academy of Science
E-mail: miroslav@biomed.bas.bg

³ Department of Information Modeling, Institute of Mathematics
and Informatics, Bulgarian Academy of Sciences

⁴ Department of Parallel Algorithms, Institute of Information
and Communication Technologies, Bulgarian Academy of Sciences
E-mail: venelin@parallel.bas.bg

Abstract: The purpose of this article is the calculation of conjunctions and disjunctions with respect to certain IF implications and negations. With constructed operations we consider algebraic structures such monoids, lattices and study their properties.

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1 Introduction

We will use defined in [1] implications to calculate their respective conjunctions and disjunctions, with respect to the rule:

$$\langle a, b \rangle \vee \langle c, d \rangle = \neg \langle a, b \rangle \rightarrow \neg \neg \langle c, d \rangle$$

$$\langle a, b \rangle \wedge \langle c, d \rangle = \neg (\neg \neg \langle a, b \rangle \rightarrow \neg \langle c, d \rangle)$$

2 Construction of Conjunctions and Disjunctions

$\vee_{2,1}$	$\langle \max(a, \min(b, c)), \min(b, d) \rangle$
$\wedge_{2,1}$	$\langle \min(a, c), \max(b, \min(a, d)) \rangle$
$\vee_{2,2}$	$\langle \overline{sg}(\overline{sg}(a) - sg(c)), \overline{sg}(c)sg(\overline{sg}(a) - sg(c)) \rangle;$
$\wedge_{2,2}$	$\langle sg(sg(a) - \overline{sg}(c)), \overline{sg}(sg(a) - \overline{sg}(c)) \rangle;$
$\vee_{2,3}$	$\langle 1 - \overline{sg}(c)sg(\overline{sg}(a) - sg(c)), \overline{sg}(c)sg(\overline{sg}(a) - sg(c)) \rangle;$
$\wedge_{2,3}$	$\langle \overline{sg}(1 - sg(c)sg(sg(a) - \overline{sg}(c))), sg(1 - sg(c)sg(sg(a) - \overline{sg}(c))) \rangle$
$\vee_{2,4}$	$\langle \max(a, c), \min(b, d) \rangle$
$\wedge_{2,4}$	$\langle \min(a, c), \max(b, d) \rangle$
$\vee_{2,5}$	$\langle \min(1, a + c), \max(0, b + d - 1) \rangle$
$\wedge_{2,5}$	$\langle \max(0, a + c - 1), \min(1, d + b) \rangle$
$\vee_{2,6}$	$\langle a + b.c, b.d \rangle$
$\wedge_{2,6}$	$\langle ac, b + ad \rangle$
$\vee_{2,7}$	$\langle \min(\max(a, b), \max(a, c), \max(c, d)), \max(\min(c, d) \min(d, b), \min(a, b)) \rangle$
$\wedge_{2,7}$	$\langle \max(\min(c, d) \min(a, c), \min(a, b)), \min(\max(a, b), \max(b, d), \max(c, d)) \rangle$
$\vee_{2,8}$	$\langle 1 - (1 - \min(sg(a), sg(c)))sg(\overline{sg}(a) - sg(c)), \max(\overline{sg}(a), \overline{sg}(c))sg(\overline{sg}(a) - sg(c))sg(\overline{sg}(c) - sg(a)) \rangle$
$\wedge_{2,8}$	$\langle \overline{sg}(1 - (1 - \min(\overline{sg}(a), \overline{sg}(c)))sg(sg(a) - \overline{sg}(c))), sg(1 - (1 - \min(\overline{sg}(a), \overline{sg}(c)))sg(sg(a) - \overline{sg}(c))) \rangle;$
$\vee_{2,9}$	$\langle ab + a^2 + b^2c(c + d), ab^2 + ba^2 + b^2d(cd + c^2 + d);$
$\wedge_{2,9}$	$\langle (ab + a^2)(b^2 + a^2b + ab^2 + (a^2 + ab)(cd + c^2)), (b^2 + a^2b + ab^2 + (ab + a^2)^2d)^2 + (b^2 + a^2b + ab^2 + (ab + a^2)^2d)(ab + a^2). (b^2 + a^2b + ab^2 + (a^2 + ab)(cd + c^2)) \rangle$
$\vee_{2,10}$	$\langle \min(c, \overline{sg}(1 - b)) + sg(1 - b)(\overline{sg}(1 - c) + \min(a, sg(1 - c))), \min(d, \overline{sg}(1 - b)) + \min(b, sg(1 - b), sg(1 - c)) \rangle$
$\wedge_{2,10}$	$\langle c.\overline{sg}(1 - a) + a.sg(1 - a).sg(1 - d), d.\overline{sg}(1 - a) + sg(1 - a).(\overline{sg}(1 - d) + b.sg(1 - d)) \rangle$
$\vee_{2,11}$	$\langle 1 - \overline{sg}(c)sg(\overline{sg}(a) - sg(c)), \overline{sg}(c)sg(\overline{sg}(a) - sg(c))sg(\overline{sg}(c) - sg(a)) \rangle$

$\wedge_{2,11}$	$\langle \overline{sg}(1 - sg(c)sg(sg(a) - \overline{sg}(c))),$ $sg(1 - sg(c)sg(sg(a) - \overline{sg}(c))) \rangle$
$\vee_{2,12}$	$\langle \max(1 - b, 1 - d), 1 - \max(1 - b, 1 - d) \rangle$
$\wedge_{2,12}$	$\langle 1 - \max(b, d), \max(b, d) \rangle$
$\vee_{2,13}$	$\langle a + c - ac, bd \rangle$
$\wedge_{2,13}$	$\langle ac, b + d - bd \rangle$
$\vee_{2,14}$	$\langle 1 - (1 - sg(1 - d))sg(\overline{sg}(1 - b) - sg(1 - d))$ $- \overline{sg}(1 - d)\overline{sg}(\overline{sg}(1 - b) - sg(1 - d))sg(\overline{sg}(1 - d)$ $- sg(1 - b)), \overline{sg}(1 - d)sg(\overline{sg}(1 - d) - sg(1 - b)) \rangle$
$\wedge_{2,14}$	$\langle \overline{sg}(1 - sg(1 - d))sg(sg(1 - d) - \overline{sg}(1 - b)),$ $sg(1 - sg(1 - d))sg(sg(1 - d) - \overline{sg}(1 - b)) \rangle;$
$\vee_{2,15}$	$\langle 1 - (1 - \min(sg(1 - b), sg(1 - d)))sg(sg(\overline{sg}(1 - b)$ $- sg(1 - d)) + sg(\overline{sg}(1 - d) - sg(1 - b)))$ $- \min(sg(1 - b), sg(1 - d))sg(\overline{sg}(1 - b) - sg(1 - d))$ $sg(\overline{sg}(1 - d) - sg(1 - b)), 1 - (1 - \max(\overline{sg}(1 - b),$ $\overline{sg}(1 - d)))sg(\overline{sg}(\overline{sg}(1 - b) - sg(1 - d))$ $+ \overline{sg}(\overline{sg}(1 - d) - sg(1 - b))) - \max(\overline{sg}(1 - b), \overline{sg}(1 - d))$ $. \overline{sg}(\overline{sg}(1 - b) - sg(1 - d))\overline{sg}(\overline{sg}(1 - d) - sg(1 - b)) \rangle$
$\wedge_{2,15}$	$\langle \overline{sg}((1 - \max(sg(1 - b), sg(1 - d)))sg(\overline{sg}(sg(1 - b)$ $- \overline{sg}(1 - d)) + \overline{sg}(sg(1 - d) - \overline{sg}(1 - b))) + \max(sg(1 - b),$ $sg(1 - d))\overline{sg}(sg(1 - b) - \overline{sg}(1 - d))\overline{sg}(sg(1 - d) - \overline{sg}(1 - b)) \rangle$
$\vee_{2,16}$	$\langle \max(sg(a), sg(c)), \min(\overline{sg}(a), \overline{sg}(c)) \rangle$
$\wedge_{2,16}$	$\langle \overline{sg}(\max(\overline{sg}(a), \overline{sg}(c))), sg(\max(\overline{sg}(a), \overline{sg}(c))) \rangle$
$\vee_{2,17}$	$\langle \max(a^2 + ab, c(c + d)),$ $\min((ab + a^2)b + b^2, d(cd + c^2 + d)) \rangle$
$\wedge_{2,17}$	$\langle \min((ab + a^2)((ab + a^2)b + b^2) + (ab + a^2)^2, c^2 + cd),$ $\max(b^2 + b(a^2 + ab), d)^2 + \max(b^2 + b(a^2 + ab),$ $d) \min((ab + a^2)((ab + a^2)b + b^2)$ $+ (ab + a^2)^2, c^2 + cd) \rangle$
$\vee_{2,18}$	$\langle \max(1 - b, 1 - d), \min(b, d) \rangle$
$\wedge_{2,18}$	$\langle 1 - \max(b, d), \max(b, d) \rangle$
$\vee_{2,19}$	$\langle \max(os(\overline{sg}(1 - b) + \overline{sg}(1 - b)),$ $\overline{sg}(d)), \min(\overline{sg}(1 - b), sg(d)) \rangle$
$\wedge_{2,19}$	$\langle \overline{sg}(\min(sg(1 - sg(1 - b)), sg(1 - d))),$ $sg(\min(sg(1 - sg(1 - b)), sg(1 - d))) \rangle$
$\vee_{2,20}$	$\langle \max(sg(a), sg(c)), \min(\overline{sg}(a), \overline{sg}(c)) \rangle$

$\wedge_{2,20}$	$\langle \overline{sg}(\max(\overline{sg}(a), \overline{sg}(c))), sg(\max(\overline{sg}(a), \overline{sg}(c))) \rangle$
$\vee_{2,21}$	$\langle \max(a^2 + ab, c(c+d)(c(c+d) + d(cd+d+c^2))),$ $\min(b(a^2+ab+b), d(cd+d+c^2)(c^2(c+d)^2$ $+d(cd+d+c^2) + c(c+d)d(cd+d+c^2))) \rangle$
$\wedge_{2,21}$	$\langle \min((a^2+ab)(b^2+b(a^2+ab)+a^2+ab),$ $(c^2+cd)(d^2+c^2+cd+(c^2+cd)d)),$ $\max(b^2+b(a^2+ab), d(d+c^2+cd))^2$ $+ \max(b^2+b(a^2+ab), d(d+c^2+cd))$ $\cdot \min((a^2+ab)(b^2+b(a^2+ab)+a^2+ab),$ $(c^2+cd)(d^2+c^2+cd+(c^2+cd)d)) \rangle$
$\vee_{2,22}$	$\langle 1 - \min(b, d), \min(b, d) \rangle$
$\wedge_{2,22}$	$\langle 1 - \max(b, d), \max(b, d) \rangle$
$\vee_{2,23}$	$\langle 1 - \min(\overline{sg}(1-b), \overline{sg}(1-d)), \min(\overline{sg}(1-b), \overline{sg}(1-d)) \rangle$
$\wedge_{2,23}$	$\langle \overline{sg}(1 - \min(\overline{sg}(1-b), \overline{sg}(1-d))),$ $\overline{sg}(1 - \min(\overline{sg}(1-b), \overline{sg}(1-d))) \rangle$
$\vee_{2,24}$	$\langle \overline{sg}(\overline{sg}(1-b) - sg(c))\overline{sg}(\overline{sg}(1-d) - sg(a)),$ $sg(\overline{sg}(1-b) - sg(c))sg(\overline{sg}(1-d) - sg(a)) \rangle$
$\wedge_{2,24}$	$\langle \overline{sg}(1 - sg(sg(a) - \overline{sg}(1-d))sg(sg(c) - \overline{sg}(1-b))),$ $sg(\overline{sg}(sg(a) - \overline{sg}(1-d))\overline{sg}(sg(c) - \overline{sg}(1-b))) \rangle$
$\vee_{2,25}$	$\langle \max(a, sg(1-b)\overline{sg}(1-a)),$ $\overline{sg}(1-c)\overline{sg}(\overline{sg}(1-d))\overline{sg}(1 - \overline{sg}(1-c)),$ $\min(\overline{sg}(1-b), \overline{sg}(1-d)) \rangle$
$\wedge_{2,25}$	$\langle \overline{sg}(1 - \min(\overline{sg}(1-a), c)),$ $\max(\overline{sg}(1-b), sg(1-a)\overline{sg}(1-b)) \rangle$
$\vee_{2,26}$	$\langle \max(sg(a), sg(c)), \min(sg(1-b), \overline{sg}(1-d)) \rangle$
$\wedge_{2,26}$	$\langle \overline{sg}(1 - \min(\overline{sg}(a), sg(c))), sg(\max(\overline{sg}(1-b), \overline{sg}(1-d))) \rangle$
$\vee_{2,27}$	$\langle \max(sg(a), sg(c)), \min(\overline{sg}(1-b), \overline{sg}(1-d)) \rangle$
$\wedge_{2,27}$	$\langle \overline{sg}(1 - \min(sg(a), sg(c))), sg(\max(\overline{sg}(1-b), \overline{sg}(1-d))) \rangle$
$\vee_{2,28}$	$\langle \max(\overline{sg}(1-a), \overline{sg}(1-c)), \min(\overline{sg}(1-b), \overline{sg}(1-d)) \rangle$
$\wedge_{2,28}$	$\langle \overline{sg}(1 - \min(\overline{sg}(1-a), c)), \max(\overline{sg}(1-b), \overline{sg}(1-d)) \rangle$
$\vee_{2,29}$	$\langle \max(\overline{sg}(1-a), \overline{sg}(1-c)), \min(\overline{sg}(1-b), \overline{sg}(1-d)) \rangle$
$\wedge_{2,29}$	$\langle \overline{sg}(1 - \min(\overline{sg}(1-a), \overline{sg}(1-c))), \max(\overline{sg}(1-b),$ $sg(1-d)) \rangle$
$\vee_{2,30}$	$\langle \max(a, \min(1-a, c)), \min(1-a, 1-c) \rangle$
$\wedge_{2,30}$	$\langle 1 - \max(1-a, \min(a, 1-c)), \max(1-a, \min(a, 1-c)) \rangle$
$\vee_{2,31}$	$\langle \overline{sg}(\overline{sg}(a) - sg(c)), \overline{sg}(c)sg(\overline{sg}(a) - sg(c)) \rangle$

$\wedge_{2,31}$	$\langle \text{sg}(\text{sg}(a) - \overline{\text{sg}}(c)), \overline{\text{sg}}(\text{sg}(a) - \overline{\text{sg}}(c)) \rangle$
$\vee_{2,32}$	$\langle 1 - \overline{\text{sg}}(c)\text{sg}(\overline{\text{sg}}(a) - \text{sg}(c)), \overline{\text{sg}}(c)\text{sg}(\overline{\text{sg}}(a) - \text{sg}(c)) \rangle$
$\wedge_{2,32}$	$\langle \overline{\text{sg}}(1 - \text{sg}(c)\text{sg}(\text{sg}(a) - \overline{\text{sg}}(c))), \text{sg}(1 - \text{sg}(c)\text{sg}(\text{sg}(a) - \overline{\text{sg}}(c))) \rangle$
$\vee_{2,33}$	$\langle 1 - \min(1 - a, 1 - c), \min(1 - a, 1 - c) \rangle$
$\wedge_{2,33}$	$\langle \min(a, c), 1 - \min(a, c) \rangle$
$\vee_{2,34}$	$\langle \min(1, a + c), \max(0, (1 - c) - a) \rangle$
$\wedge_{2,34}$	$\langle 1 - \min(1, 2 - a - c), \min(1, 2 - a - c) \rangle$
$\vee_{2,35}$	$\langle 1 - (1 - a)(1 - c), (1 - a)(1 - c) \rangle$
$\wedge_{2,35}$	$\langle ac, 1 - ac \rangle$
$\vee_{2,36}$	$\langle \min(1 - \min(1 - a, 1 - c), \max(a, 1 - a), \max(c, (1 - c))), \max(\min(1 - a, (1 - c)), \min(a, 1 - a), \min(c, (1 - c))) \rangle$
$\vee_{2,37}$	$\langle 1 - \max(\overline{\text{sg}}(a), \overline{\text{sg}}(c)).\text{sg}(\overline{\text{sg}}(a) - \text{sg}(c)), \max(\overline{\text{sg}}(a), \overline{\text{sg}}(c)).\text{sg}(\overline{\text{sg}}(a) - \text{sg}(c)) \rangle$
$\wedge_{2,37}$	$\langle \overline{\text{sg}}(1 - \max(\text{sg}(a), \text{sg}(c)).\text{sg}(\text{sg}(a) - \overline{\text{sg}}(c))), \text{sg}(1 - \max(\text{sg}(a), \text{sg}(c)).\text{sg}(\text{sg}(a) - \overline{\text{sg}}(c))) \rangle$
$\vee_{2,38}$	$\langle a + (1 - a)^2 c, a(1 - a) + (1 - a)^2(1 - c) \rangle$
$\wedge_{2,38}$	$\langle a - a^2(1 - c), 1 - a + a^2(1 - c) \rangle$
$\vee_{2,39}$	$\langle (1 - (1 - c))\overline{\text{sg}}(a) + \text{sg}(a)(\overline{\text{sg}}((1 - c)) + (a)\text{sg}((1 - c))), (1 - c)\overline{\text{sg}}(a) + \text{asg}(a)\text{sg}((1 - c)) \rangle$
$\wedge_{2,39}$	$\langle 1 - (1 - c)\overline{\text{sg}}(1 - a) - \text{sg}(1 - a)(\overline{\text{sg}}(c) + (1 - a)\text{sg}(c)), (1 - c)\overline{\text{sg}}(1 - a) + \text{sg}(1 - a)(\overline{\text{sg}}(c) + (1 - a)\text{sg}(c)) \rangle$
$\vee_{2,40}$	$\langle \overline{\text{sg}}(\overline{\text{sg}}(a) - \text{sg}(c)), \text{sg}(\overline{\text{sg}}(a) - \text{sg}(c)) \rangle$
$\wedge_{2,40}$	$\langle \text{sg}(\text{sg}(a) - \overline{\text{sg}}(c)), \overline{\text{sg}}(\text{sg}(a) - \overline{\text{sg}}(c)) \rangle$
$\vee_{2,41}$	$\langle \max(\text{sg}(a), 1 - \overline{\text{sg}}(c)), \min(\overline{\text{sg}}(a), \overline{\text{sg}}(c)) \rangle$
$\wedge_{2,41}$	$\langle \overline{\text{sg}}(\max(\overline{\text{sg}}(a), \overline{\text{sg}}(c))), \text{sg}(\max(\overline{\text{sg}}(a), \overline{\text{sg}}(c))) \rangle$
$\vee_{2,42}$	$\langle \max(\text{sg}(a), \text{sg}(c)), \min(\overline{\text{sg}}(a), \overline{\text{sg}}(c)) \rangle$
$\wedge_{2,42}$	$\langle \overline{\text{sg}}(\max(\overline{\text{sg}}(a), \overline{\text{sg}}(c))), \text{sg}(\max(\overline{\text{sg}}(a), \overline{\text{sg}}(c))) \rangle$
$\vee_{2,43}$	$\langle \max(\text{sg}(a), \text{sg}(c)), \min(\overline{\text{sg}}(a), \overline{\text{sg}}(c)) \rangle$
$\wedge_{2,43}$	$\langle \overline{\text{sg}}(\max(\overline{\text{sg}}(a), 1 - c)), \max(\overline{\text{sg}}(a), 1 - c) \rangle$
$\vee_{2,44}$	$\langle \max(\text{sg}(a), \text{sg}(c)), \min(\overline{\text{sg}}(a), \overline{\text{sg}}(c)) \rangle$
$\wedge_{2,44}$	$\langle \overline{\text{sg}}(\max(\overline{\text{sg}}(a), 1 - c)), \max(\overline{\text{sg}}(a), 1 - c) \rangle$
$\vee_{2,45}$	$\langle \max(\text{sg}(a), \text{sg}(c)), \min(\overline{\text{sg}}(a), \overline{\text{sg}}(c)) \rangle$
$\wedge_{2,45}$	$\langle \overline{\text{sg}}(\max(\overline{\text{sg}}(a), \overline{\text{sg}}(c))), \max(\overline{\text{sg}}(a), \overline{\text{sg}}(c)) \rangle$
$\vee_{2,46}$	$\langle \max(1 - b, \min(b, 1 - d)), \min(b, d) \rangle$

$\wedge_{2,46}$	$\langle 1 - \max(b, d), \max(b, d) \rangle$
$\vee_{2,47}$	$\langle \overline{sg}(\overline{sg}(1-b) - sg(1-d)),$ $\overline{sg}(1-d)sg(\overline{sg}(1-b) - sg(1-d)) \rangle$
$\wedge_{2,47}$	$\langle \overline{sg}(1 - sg(1-d)sg(sg(1-b) - \overline{sg}(1-d))),$ $sg(1 - sg(1-d)sg(sg(1-b) - \overline{sg}(1-d))) \rangle$
$\vee_{2,48}$	$\langle 1 - \overline{sg}(1-d)sg(\overline{sg}(1-b) - sg(1-d)),$ $\overline{sg}(1-d)sg(\overline{sg}(1-b) - sg(1-d)) \rangle$
$\wedge_{2,48}$	$\langle \overline{sg}(1 - sg(1-d)sg(sg(1-b) - \overline{sg}(1-d))),$ $sg(1 - sg(1-d)sg(sg(1-b) - \overline{sg}(1-d))) \rangle$
$\vee_{2,49}$	$\langle \min(1, 2 - b - d), \max(0, b - 1 + d) \rangle$
$\wedge_{2,49}$	$\langle \max(0, 1 - b - d), 1 - \max(0, 1 - b - d) \rangle$
$\vee_{2,50}$	$\langle 1 - b + b(1-d), b - b(1-d) \rangle$
$\wedge_{2,50}$	$\langle (1-b)(1-d), 1 - (1-b)(1-d) \rangle$
$\vee_{2,51}$	$\langle \min(\max(1-b, 1-d), \max(1-b, b), \max(1-d, d)),$ $\max(1 - \max(1-b, 1-d), \min(1-b, b), \min(1-d, d)) \rangle$
$\wedge_{2,51}$	$\langle \max(1 - \max(b, d), \min(1-b, b), \min(d, 1-d)),$ $1 - \max(1 - \max(b, d), \min(1-b, b), \min(d, 1-d)) \rangle$
$\vee_{2,52}$	$\langle 1 - (1 - \min(sg(1-b), sg(1-d)))sg(\overline{sg}(1-b)$ $- sg(1-d)), 1 - \min(sg(1-b), sg(1-d))sg(\overline{sg}(1-b)$ $- sg(1-d)) \rangle$
$\wedge_{2,52}$	$\langle \overline{sg}(\min(\overline{sg}(1-b), \overline{sg}(1-d))sg(sg(1-b) - \overline{sg}(1-d))),$ $sg(\min(\overline{sg}(1-b), \overline{sg}(1-d))sg(sg(1-b) - \overline{sg}(1-d))) \rangle$
$\vee_{2,53}$	$\langle 1 - b + b^2(1-d), (1-b)b + b^2d \rangle$
$\wedge_{2,53}$	$\langle (1-b)b + (1-b)^2(1-d), 1 - (1-b)b - (1-b)^2(1-d) \rangle$
$\vee_{2,54}$	$\langle (1-d)\overline{sg}(1-b) + sg(1-b)(\overline{sg}(d) + (1-b)sg(d)),$ $(1 - (1-d))\overline{sg}(1-b) + bsg(b)sg(1 - (1-d)) \rangle$
$\wedge_{2,54}$	$\langle (1-d)\overline{sg}(1-b) + bsg(b)sg(1-d),$ $1 - (1-d)\overline{sg}(1-b) - bsg(b)sg(1-d) \rangle$
$\vee_{2,55}$	$\langle \overline{sg}(\overline{sg}(1-b) - sg(1-d)), sg(\overline{sg}(1-b) - sg(1-d)) \rangle$
$\wedge_{2,55}$	$\langle sg(sg(1-b) - \overline{sg}(1-d)), \overline{sg}(sg(1-b) - \overline{sg}(1-d)) \rangle$
$\vee_{2,56}$	$\langle \max(sg(1-b), \overline{sg}(d)), \min(\overline{sg}(1-b), 1 - \overline{sg}(d)) \rangle$
$\wedge_{2,56}$	$\langle \overline{sg}(1 - \min(\overline{sg}(1-b), sg(1-d))),$ $sg(1 - \min(\overline{sg}(1-b), sg(1-d))) \rangle$
$\vee_{2,57}$	$\langle \max(sg(1-b), sg(1-d)), \min(\overline{sg}(1-b), \overline{sg}(1-d)) \rangle$
$\wedge_{2,57}$	$\langle \overline{sg}(1 - \min(sg(1-b), sg(1-d))),$ $sg(1 - \min(sg(1-b), sg(1-d))) \rangle$

$\vee_{2,58}$	$\langle \max(\overline{sg}(b), \overline{sg}(1 - \overline{sg}(d))), 1 - \max(1 - b, \overline{sg}(d)) \rangle$
$\wedge_{2,58}$	$\langle \overline{sg}(\max(b, \overline{sg}(1 - d))), \max(b, \overline{sg}(1 - d)) \rangle$
$\vee_{2,59}$	$\langle \max(\overline{sg}(b), \overline{sg}(d)), 1 - \max(1 - b, \overline{sg}(d)) \rangle$
$\wedge_{2,59}$	$\langle \overline{sg}(\max(b, \overline{sg}(1 - d))), \max(b, \overline{sg}(1 - d)) \rangle$
$\vee_{2,60}$	$\langle \max(\overline{sg}(b), \overline{sg}(d)), \min(b, sg(d)) \rangle$
$\wedge_{2,60}$	$\langle \overline{sg}(1 - \min(1 - b, sg(1 - d))), 1 - \min(1 - b, sg(1 - d)) \rangle$
$\vee_{2,61}$	$\langle \max(c, \min(a, d)), \min(b, d) \rangle$
$\wedge_{2,61}$	$\langle \min(a, c), \max(d, \min(b, c)) \rangle$
$\vee_{2,62}$	$\langle \overline{sg}(\overline{sg}(1 - d) - a), \overline{sg}(1 - b)sg(\overline{sg}(1 - d) - a) \rangle$
$\wedge_{2,62}$	$\langle \overline{sg}(1 - \overline{sg}(1 - a)sg(c - \overline{sg}(1 - b))), \overline{sg}(c - \overline{sg}(1 - b)) \rangle$
$\vee_{2,63}$	$\langle 1 - (1 - a)sg(d - a), bsg(d - a) \rangle$
$\wedge_{2,63}$	$\langle asg(c - b), 1 - (1 - b)sg(c - b) \rangle$
$\vee_{2,64}$	$\langle c + ad, bd \rangle$
$\wedge_{2,64}$	$\langle ac, d + bc \rangle$
$\vee_{2,65}$	$\langle 1 - (1 - \min(sg(a), sg(c)))sg(\overline{sg}(1 - d) - sg(a)), \max(\overline{sg}(1 - b), \overline{sg}(1 - d))sg(\overline{sg}(1 - d) - sg(a))sg(\overline{sg}(1 - b) - sg(c)) \rangle$
$\wedge_{2,65}$	$\langle \overline{sg}(1 - \max(sg(a), sg(c)))sg(sg(c) - \overline{sg}(1 - b))sg(sg(a) - \overline{sg}(1 - d)), sg(1 - (1 - \min(\overline{sg}(1 - b), \overline{sg}(1 - d)))sg(sg(c) - \overline{sg}(1 - b))) \rangle$
$\vee_{2,66}$	$\langle c + d^2a, ad + d^2b \rangle$
$\wedge_{2,66}$	$\langle bc + c^2a, d + c^2b \rangle$
$\vee_{2,67}$	$\langle asg(1 - d) + sg(1 - d)(\overline{sg}(1 - a) + csg(1 - a)), b\overline{sg}(1 - d) + dsg(1 - d)sg(1 - a) \rangle$
$\wedge_{2,67}$	$\langle a\overline{sg}(1 - c) + dsg(1 - c)sg(1 - b), b\overline{sg}(1 - c) + sg(1 - c)(\overline{sg}(1 - b) + dsg(1 - b)) \rangle$
$\vee_{2,68}$	$\langle 1 - (1 - a)sg(d - a), bsg(d - a)sg(b - c) \rangle$
$\wedge_{2,68}$	$\langle asg(c - b)sg(a - d), 1 - (1 - b)sg(c - b) \rangle$
$\vee_{2,69}$	$\langle 1 - (1 - a)sg(d - a) - b\overline{sg}(d - a)sg(b - c), bsg(b - c) \rangle$
$\wedge_{2,69}$	$\langle asg(a - d), 1 - (1 - b)sg(c - b) - a\overline{sg}(c - b)sg(a - d) \rangle$
$\vee_{2,70}$	$\langle \max(\overline{sg}(d), a), \min(sg(d), b) \rangle$
$\wedge_{2,70}$	$\langle \min(sg(c), a), \max(\overline{sg}(c), b) \rangle$
$\vee_{2,71}$	$\langle \max(c, a), \min(dc + d^2, b) \rangle$
$\wedge_{2,71}$	$\langle \min(cd + c^2, a), \max(b, d) \rangle$

$\vee_{2,72}$	$\langle \max(a, c), \min(1 - c, b) \rangle$
$\wedge_{2,72}$	$\langle \min(1 - d, a), \max(b, d) \rangle$
$\vee_{2,73}$	$\langle \max(1 - \max(\text{sg}(d), \text{sg}(1 - c)), a), \min(\text{sg}(1 - c), b) \rangle$
$\wedge_{2,73}$	$\langle \min(\text{sg}(1 - d), a), \max(1 - \max(\text{sg}(c), \text{sg}(1 - d)), b) \rangle$
$\vee_{2,74}$	$\langle \max(\overline{\text{sg}}(b), \overline{\text{sg}}(d)), \min(\text{sg}(b), \text{sg}(d)) \rangle$
$\wedge_{2,74}$	$\langle \text{sg}(\min(\overline{\text{sg}}(b), \overline{\text{sg}}(d))), \overline{\text{sg}}(\min(\overline{\text{sg}}(b), \overline{\text{sg}}(d))) \rangle$
$\vee_{2,75}$	$\langle \max \min(1, cd^2 + c^2(d + 1))(\min(1, cd^2 + c^2(d + 1)) + d(d + c)), (a^2b + ab^2 + a^2)(b^2 + ab + a^2b + ab^2 + a^2)), \min(\min(1, d(d + c)(r^2 + d(d + c))) \cdot (\min(1, cd^2 + c^2(d + 1))(\min(1, cd^2 + c^2(d + 1)) + d(d + c))), (b^2 + ab)((a^2b + ab^2 + a^2)^2 + b^2 + ab) + (b^2 + ab)(a^2b + ab^2 + a^2)) \rangle$
$\wedge_{2,75}$	$\langle \min((cd^2 + c^2 + c^2d)(d^2 + cd + cd^2 + c^2 + c^2d), (ab^2 + a^2b + a^2)(ab^2 + a^2b + a^2 + b^2 + ab)((b^2 + a)^2 + [(b^2 + a)(ab^2 + a^2b + a^2 + 1) + (ab^2 + a^2b + a^2)^2]^2 + (ab^2 + a^2b + a^2)(ab^2 + a^2b + a^2 + b^2 + ab)) + (ab^2 + a^2b + a^2)(ab^2 + a^2b + a^2 + b^2 + ab)(b^2 + a)[(b^2 + a) \cdot (ab^2 + a^2b + a^2 + 1) + (ab^2 + a^2b + a^2)^2]^2 + \max(d^2 + cd, (b^2 + a)[(b^2 + a)(ab^2 + a^2b + a^2 + 1) + (ab^2 + a^2b + a^2)^2] + (ab^2 + a^2b + a^2)(ab^2 + a^2b + a^2 + b^2 + ab) + (b^2 + a)[(b^2 + a)(ab^2 + a^2b + a^2 + 1) + (ab^2 + a^2b + a^2)^2])) \min((cd^2 + c^2 + c^2d)(d^2 + cd + cd^2 + c^2 + c^2d), (ab^2 + a^2b + a^2)(ab^2 + a^2b + a^2 + b^2 + ab)((b^2 + a)^2 + [(b^2 + a)(ab^2 + a^2b + a^2 + 1) + (ab^2 + a^2b + a^2)^2]^2 + (ab^2 + a^2b + a^2)(ab^2 + a^2b + a^2 + b^2 + ab) + (ab^2 + a^2b + a^2)(ab^2 + a^2b + a^2 + b^2 + ab)(b^2 + a)[(b^2 + a) \cdot (ab^2 + a^2b + a^2 + 1) + (ab^2 + a^2b + a^2)^2]^2 + \max(d^2 + cd, (b^2 + a)[(b^2 + a)(ab^2 + a^2b + a^2 + 1) + (ab^2 + a^2b + a^2)^2] + (ab^2 + a^2b + a^2)(ab^2 + a^2b + a^2 + b^2 + ab) + (b^2 + a)[(b^2 + a)(ab^2 + a^2b + a^2 + 1) + (ab^2 + a^2b + a^2)^2]^2 + (ab^2 + a^2b + a^2)(ab^2 + a^2b + a^2 + b^2 + ab)(b^2 + a)[(b^2 + a) \cdot (ab^2 + a^2b + a^2 + 1) + (ab^2 + a^2b + a^2)^2]^2]) \rangle$

	$\begin{aligned} & \cdot(ab^2 + a^2b + a^2 + 1) + (ab^2 + a^2b + a^2)^2]) + \max(d^2 \\ & + cd, (b^2 + a)[(b^2 + a)(ab^2 + a^2b + a^2 + 1) + (ab^2 + a^2b \\ & + a^2)^2]((ab^2 + a^2b + a^2)(ab^2 + a^2b + a^2 + b^2 + ab) + (b^2 \\ & + a)[(b^2 + a)(ab^2 + a^2b + a^2 + 1) + (ab^2 + a^2b + a^2)^2])) \\ & \cdot \min((cd^2 + c^2 + c^2d)(d^2 + cd + cd^2 + c^2 + c^2d), \\ & (ab^2 + a^2b + a^2)(ab^2 + a^2b + a^2 + b^2 + ab)((b^2 + a)^2 \\ & [(b^2 + a)(ab^2 + a^2b + a^2 + 1) + (ab^2 + a^2b + a^2)^2]^2 \\ & +(ab^2 + a^2b + a^2)(ab^2 + a^2b + a^2 + b^2 + ab)) \\ & +(ab^2 + a^2b + a^2)(ab^2 + a^2b + a^2 + b^2 + ab)(b^2 \\ & + a)[(b^2 + a)(ab^2 + a^2b + a^2 + 1) + (ab^2 + a^2b + a^2)^2])^2 \\ & + \max(d^2 + cd, (b^2 + a)[(b^2 + a)(ab^2 + a^2b + a^2 + 1) \\ & +(ab^2 + a^2b + a^2)^2]((ab^2 + a^2b + a^2)^2) \\ & (ab^2 + a^2b + a^2 + b^2 + ab) + (b^2 + a)[(b^2 + a) \\ & .(ab^2 + a^2b + a^2 + 1) + (ab^2 + a^2b + a^2)^2]))^2 \end{aligned}$
$\vee_{2,76}$	$\langle \max(c, a), 1 - \max(c, a) \rangle$
$\wedge_{2,76}$	$\langle 1 - \max(1 - c, 1 - a), \max(1 - c, 1 - a) \rangle$
$\vee_{2,77}$	$\langle 1 - \min(\text{sg}(1 - a), \text{sg}(1 - c)), \min(\text{sg}(1 - a), \text{sg}(1 - c)) \rangle$
$\wedge_{2,77}$	$\langle \text{sg}(\min(\overline{\text{sg}}(1 - a), \overline{\text{sg}}(1 - c))), \overline{\text{sg}}(\min(\overline{\text{sg}}(1 - a), \overline{\text{sg}}(1 - c))) \rangle$
$\vee_{2,78}$	$\langle \max(\overline{\text{sg}}(1 - c), a), \min(\text{sg}(d), b) \rangle$
$\wedge_{2,78}$	$\langle \min(\text{sg}(c), a), \max(\overline{\text{sg}}(1 - d), b) \rangle$
$\vee_{2,79}$	$\langle \max(\overline{\text{sg}}(1 - c), \overline{\text{sg}}(1 - a)), \overline{\text{sg}}(\min(\text{sg}(d), \text{sg}(b))) \rangle$
$\wedge_{2,79}$	$\langle \text{sg}(\min(\overline{\text{sg}}(1 - c), \overline{\text{sg}}(1 - a))), \overline{\text{sg}}(1 - \max(\text{sg}(d), \text{sg}(b))) \rangle$
$\vee_{2,80}$	$\langle \max(\overline{\text{sg}}(1 - c), a), \min(d, b) \rangle$
$\wedge_{2,80}$	$\langle \min(c, a), \max(\overline{\text{sg}}(1 - d), b) \rangle$
$\vee_{2,81}$	$\langle \max(\overline{\text{sg}}(1 - a), \overline{\text{sg}}(1 - c)), \min(\overline{\text{sg}}(1 - d), \overline{\text{sg}}(1 - b)) \rangle$
$\wedge_{2,81}$	$\langle \overline{\text{sg}}(1 - \min(\overline{\text{sg}}(1 - c), \overline{\text{sg}}(1 - a))), \overline{\text{sg}}(1 - \max(\overline{\text{sg}}(1 - b), \overline{\text{sg}}(1 - d))) \rangle$
$\vee_{2,82}$	$\langle \max(c, \min(1 - c, a)), \min(1 - c, 1 - a) \rangle$
$\wedge_{2,82}$	$\langle 1 - \max(1 - c, \min(c, 1 - a)), \max(1 - c, \min(c, 1 - a)) \rangle$
$\vee_{2,83}$	$\langle \overline{\text{sg}}(\overline{\text{sg}}(a) + \overline{\text{sg}}(c) - 1), \overline{\text{sg}}(a)\text{sg}(\overline{\text{sg}}(a) + \overline{\text{sg}}(c) - 1) \rangle$
$\wedge_{2,83}$	$\langle \text{sg}(-\overline{\text{sg}}(a) + c), \overline{\text{sg}}(-\overline{\text{sg}}(a) + c) \rangle$
$\vee_{2,84}$	$\langle 1 - (1 - a)\text{sg}(1 - c - a), (1 - a)\text{sg}(1 - c - a) \rangle$
$\wedge_{2,84}$	$\langle \text{asg}(c + a - 1), 1 - \text{asg}(c + a - 1) \rangle$
$\vee_{2,85}$	$\langle c + (1 - c)^2a, (1 - c)c + (1 - c)^2 \rangle$
$\wedge_{2,85}$	$\langle c - c^2(1 - a), 1 - c + c^2(1 - a) \rangle$

$\vee_{2,86}$	$\langle a\bar{sg}(c) + sg(c)(\bar{sg}(1-a) + (c)sg((1-c))),$ $(1-a)\bar{sg}(c) + (1-c)sg(c)sg(1-a) \rangle$
$\wedge_{2,86}$	$\langle 1 - (1-a)\bar{sg}(1-c) + sg(1-c)(\bar{sg}(a) + (1-c)sg(c)),$ $(1-a)\bar{sg}(1-c) + sg(1-c)(\bar{sg}(a) + (1-c)sg(c)) \rangle$
$\vee_{2,87}$	$\langle \max(\bar{sg}(1-c), a), \min(sg(1-c), 1-a) \rangle$
$\wedge_{2,87}$	$\langle 1 - \max(\bar{sg}(c), 1-a), \max(\bar{sg}(c), 1-a) \rangle$
$\vee_{2,88}$	$\langle \max(\bar{sg}(1-c), \bar{sg}(1-a)), \min((sg(1-c)), sg(1-a)) \rangle$
$\wedge_{2,88}$	$\langle sg(1 - \max(sg(1-c), sg(1-a))),$ $\bar{sg}(1 - \max(sg(1-c), sg(1-a))) \rangle$
$\vee_{2,89}$	$\langle \max(\bar{sg}((1-c)), a), \min(1-c, 1-a) \rangle$
$\wedge_{2,89}$	$\langle 1 - \max(\bar{sg}(c), 1-a), \max(\bar{sg}(c), 1-a) \rangle$
$\vee_{2,90}$	$\langle \max(sg(a), sg(c)), \min(\bar{sg}(c), \bar{sg}(a)) \rangle$
$\wedge_{2,90}$	$\langle \bar{sg}(\max(\bar{sg}(a), sg(1-c))), \bar{sg}(1 - \max(\bar{sg}(a), sg(1-c))) \rangle$
$\vee_{2,91}$	$\langle \max((1-d), \min(d, 1-b)), 1 - \max(1-b, (1-d)) \rangle$
$\wedge_{2,91}$	$\langle 1 - \max(b, d), \max(b, d) \rangle$
$\vee_{2,92}$	$\langle \bar{sg}(b - \bar{sg}(d)), \min(b, sg(b - \bar{sg}(d))) \rangle$
$\wedge_{2,92}$	$\langle \bar{sg}(1 - \min(1-b, sg(b - \bar{sg}(1-d)))),$ $1 - \min(1-b, sg(b - \bar{sg}(1-d))) \rangle$
$\vee_{2,93}$	$\langle (1 - \min(b, sg(b+d-1)), \min(b, sg(b+d-1)) \rangle$
$\wedge_{2,93}$	$\langle \min(1-b, sg(1-b-d)), 1 - \min(1-b, sg(1-b-d)) \rangle$
$\vee_{2,94}$	$\langle (1-d) + d^2(1-b), d(1-d) + d^2b \rangle$
$\wedge_{2,94}$	$\langle (1-d)d + (1-d)^2(1-b),$ $1 - (1-d)d - (1-d)^2(1-b) \rangle$
$\vee_{2,95}$	$\langle \min(1-b, \bar{sg}((1-d))) + sg((1-d))(\bar{sg}(b)$ $+ \min((1-d), sg(b))), \min(b, \bar{sg}((1-d)))$ $+ \min(d, sg((1-d)), sg(b)) \rangle$
$\wedge_{2,95}$	$\langle \min(b, \bar{sg}(d)) + \min(1-d, sg(d), sg(b)),$ $1 - \min(b, \bar{sg}(d)) - \min(1-d, sg(d), sg(b)) \rangle$
$\vee_{2,96}$	$\langle \max(\bar{sg}(d), 1-b), \min(sg(b), d) \rangle$
$\wedge_{2,96}$	$\langle \min(sg(1-b), 1-d), 1 - \min(sg(b), 1-d) \rangle$
$\vee_{2,97}$	$\langle \max(\bar{sg}(d), \bar{sg}(b)), \min(sg(d), sg(b)) \rangle$
$\wedge_{2,97}$	$\langle sg(\min(\bar{sg}(d), \bar{sg}(b))), \bar{sg}(\min(\bar{sg}(d), \bar{sg}(b))) \rangle$
$\vee_{2,98}$	$\langle \max(\bar{sg}(d), 1-b), 1 - \max(1-b, 1-d) \rangle$
$\wedge_{2,98}$	$\langle 1 - \max(b, d), \max(b, d) \rangle$
$\vee_{2,99}$	$\langle \max(\bar{sg}((d)), \bar{sg}(b)), \min(sg(d), sg(b)) \rangle$
$\wedge_{2,99}$	$\langle \bar{sg}(1 - \min(\bar{sg}(1-d), sg(b))), \bar{sg}(\min(\bar{sg}(1-d), sg(b))) \rangle$

$\vee_{2,100}$	$\langle \max(\min(asg(b), sg(ab)), csg(cd)),$ $\min(bsg(a), sg(ab), dsg(cd)) \rangle$
$\wedge_{2,100}$	$\langle \min(asg(ab), sg(ab^2), csg(d))sg(\max(\min(bsg(ab),$ $sg(a^2b)), dsg(c))), \max(\min(bsg(ab), sg(a^2b)),$ $dsg(c))sg(\min(asg(ab), sg(ab^2), csg(d))) \rangle$
$\vee_{2,101}$	$\langle 0, 0 \rangle$
$\wedge_{2,101}$	$\langle 0, 0 \rangle$
$\vee_{2,102}$	$\langle 0, 0 \rangle$
$\wedge_{2,102}$	$\langle 0, 0 \rangle$
$\vee_{2,103}$	$\langle \max(\min(1 - \min(1 - a, sg(a)), sg(\min(1 - a, sg(a)))),$ $1 - \min(\min(1 - c, sg(c)), sg(1 - \min(1 - c, sg(c))))),$ $\min(\min(1 - a, sg(a)), sg(1 - \min(1 - a, sg(a)))),$ $\min(\min(1 - c, sg(c)), sg(1 - \min(1 - c, sg(c)))) \rangle$
$\wedge_{2,103}$	$\langle \min(1 - \max(\min((1 - \min((1 - a), sg(a)))),$ $sg(\min((1 - a), sg(a)))), 1 - \min((c), sg(1 - c))),$ $sg(\max(\min((1 - \min((1 - a), sg(a)))),$ $sg(\min((1 - a), sg(a)))), 1 - \min((c), sg(1 - c)))),$ $\min(sg(1 - \max(\min((1 - \min((1 - a), sg(a)))),$ $sg(\min((1 - a), sg(a)))), 1 - \min((c), sg(1 - c)))),$ $, (max(\min((1 - \min((1 - a), sg(a)))),$ $sg(\min((1 - a), sg(a)))), 1 - \min((c), sg(1 - c)))) \rangle$
$\vee_{2,104}$	$\langle \min(1 - \min(1 - a, sg(a)), sg(\min(1 - a, sg(a)))), 0 \rangle$
$\wedge_{2,104}$	$\langle \min(1 - \min(1 - \min(1 - \min(1 - a, sg(a)))),$ $sg(\min(1 - a, sg(a)))), sg(\min((1 - \min(1 - a, sg(a)))),$ $sg(\min(1 - a, sg(a)))), sg(\min(1 - \min((1 -$ $- \min(1 - a, sg(a)))), sg(\min(1 - a, sg(a)))),$ $sg(\min(1 - \min(1 - a, sg(a)), sg(\min(1 - a,$ $sg(a)))))), 0 \rangle$
$\vee_{2,105}$	$\langle a, 0 \rangle$
$\wedge_{2,105}$	$\langle a, 0 \rangle$
$\vee_{2,106}$	$\langle \max(\min(\min(b, sg(1 - b)), sg(1 - \min(1 - b, sg(b)))),$ $\min(\min(sg(d), 1 - d), sg(1 - \min(sg(d), 1 - d)))),$ $\min(1 - \min(1 - b, sg(b)), sg(\min(1 - b, sg(b)))),$ $1 - \min(\min(sg(d), 1 - d), sg(1 - \min(sg(d), 1 - d)))) \rangle$
$\wedge_{2,106}$	$\langle \min(\min(1 - \min(1 - \min(1 - b, sg(b)), sg(\min(1 - b, sg(b)))),$ $sg(\min(1 - \min(1 - b, sg(b)), sg(\min(1 - b, sg(b))))),$

	$ 1 - \min(1 - d, \text{sg}(d))), \text{sg}(1 - \min(1 - \min(1 - b, \text{sg}(b)), \text{sg}(\min(1 - b, \text{sg}(b)))), \text{sg}(\min(1 - \min(1 - b, \text{sg}(b))), \text{sg}(\min(1 - b, \text{sg}(b)))), 1 - \min(1 - d, \text{sg}(d))))),$ $\min(1 - \min(1 - \min(1 - \min(1 - b, \text{sg}(b)), \text{sg}(\min(1 - b, \text{sg}(b)))), \text{sg}(\min(1 - \min(1 - b, \text{sg}(b))), \text{sg}(\min(1 - b, \text{sg}(b)))), 1 - \min(1 - d, \text{sg}(d))))),$ $\langle 1 - \min(1 - d, \text{sg}(d))), \text{sg}(\min(1 - \min(1 - b, \text{sg}(b)), \text{sg}(\min(1 - b, \text{sg}(b)))), \text{sg}(\min(1 - b, \text{sg}(b)))), 1 - \min(1 - d, \text{sg}(d))))\rangle$
$\vee_{2,107}$	$\langle 0, 0 \rangle$
$\wedge_{2,107}$	$\langle 0, 0 \rangle$
$\vee_{2,108}$	$\langle 0, 0 \rangle$
$\wedge_{2,108}$	$\langle \min(1 - d, \text{sg}(d)), 0 \rangle$
$\vee_{2,109}$	$\langle ab + \overline{s}\bar{g}(1 - a) + \min(\overline{s}\bar{g}(1 - b), cd + \overline{s}\bar{g}(1 - c)),$ $(ab + \overline{s}\bar{g}(1 - a))b + \min(\overline{s}\bar{g}(1 - b), d(cd + \overline{s}\bar{g}(1 - c))$ $+ \overline{s}\bar{g}(1 - d)) \rangle$
$\wedge_{2,109}$	$\langle ((ab + \overline{s}\bar{g}(1 - a))((ab + \overline{s}\bar{g}(1 - a))b + \overline{s}\bar{g}(1 - b))$ $+ \min(\overline{s}\bar{g}(1 - (ab + \overline{s}\bar{g}(1 - a))), (cd + \overline{s}\bar{g}(1 - c))),$ $((ab + \overline{s}\bar{g}(1 - a))b + \overline{s}\bar{g}(1 - b)) + \min(\overline{s}\bar{g}(1 - (ab$ $+ \overline{s}\bar{g}(1 - a))), d))((ab + \overline{s}\bar{g}(1 - a))((ab$ $+ \overline{s}\bar{g}(1 - a))b + \overline{s}\bar{g}(1 - b)) + \min(\overline{s}\bar{g}(1$ $- (ab + \overline{s}\bar{g}(1 - a))), (cd + \overline{s}\bar{g}(1 - c)))$ $+ \overline{s}\bar{g}(1 - ((ab + \overline{s}\bar{g}(1 - a))b + \overline{s}\bar{g}(1 - b))$ $- \min(\overline{s}\bar{g}(1 - (ab + \overline{s}\bar{g}(1 - a))), d)) \rangle$
$\vee_{2,110}$	$\langle \max(ab + \overline{s}\bar{g}(1 - a), cd + \overline{s}\bar{g}(1 - c)),$ $\min((ab + \overline{s}\bar{g}(1 - a))^2 + \overline{s}\bar{g}(-ab + \text{sg}(1 - a)),$ $d(cd + \overline{s}\bar{g}(1 - c)) + \overline{s}\bar{g}(1 - d)) \rangle$
$\wedge_{2,110}$	$\langle \min((ab + \overline{s}\bar{g}(1 - a))((ab + \overline{s}\bar{g}(1 - a))b + \overline{s}\bar{g}(1 - b))$ $+ \overline{s}\bar{g}(1 - (ab + \overline{s}\bar{g}(1 - a))), (cd + \overline{s}\bar{g}(1 - c))),$ $+ \overline{s}\bar{g}(1 - \max(((ab + \overline{s}\bar{g}(1 - a))b + \overline{s}\bar{g}(1 - b)), d)) \rangle$
$\vee_{2,111}$	$\langle \max(ab + \overline{s}\bar{g}(1 - a), (cd + \overline{s}\bar{g}(1 - c))(d(cd + \overline{s}\bar{g}(1 - c))$ $\max(((ab + \overline{s}\bar{g}(1 - a))b + \overline{s}\bar{g}(1 - b)),$ $d). \min((ab + \overline{s}\bar{g}(1 - a))((ab + \overline{s}\bar{g}(1 - a))b$ $+ \overline{s}\bar{g}(1 - b)) + \overline{s}\bar{g}(1 - (ab + \overline{s}\bar{g}(1 - a))), (cd + \overline{s}\bar{g}(1 - c)))$ $+ \overline{s}\bar{g}(1 - d)) + \overline{s}\bar{g}(1 - c)), \min((ab + \overline{s}\bar{g}(1 - a))b$ $+ \overline{s}\bar{g}(1 - b), d(cd + \overline{s}\bar{g}(1 - c)) + \overline{s}\bar{g}(1 - d)) \rangle$

$\wedge_{2,111}$	$\langle \min((ab + \bar{sg}(1-a))((ab + \bar{sg}(1-a))b + \bar{sg}(1-b))$ $+ \bar{sg}(1 - (ab + \bar{sg}(1-a))), (cd + \bar{sg}(1-c))((cd$ $+ \bar{sg}(1-c))d + \bar{sg}(1-d)) + \bar{sg}(1 - (cd + \bar{sg}(1-c)))),$ $\max(((ab + \bar{sg}(1-a))b + \bar{sg}(1-b)),$ $(cd + \bar{sg}(1-c))d + \bar{sg}(1-d))$ $\cdot \min((ab + \bar{sg}(1-a))((ab + \bar{sg}(1-a))b +$ $\bar{sg}(1-b)) + \bar{sg}(1 - (ab + \bar{sg}(1-a))),$ $(cd + \bar{sg}(1-c))((cd + \bar{sg}(1-c))d + \bar{sg}(1-d))$ $+ \bar{sg}(1 - (cd + \bar{sg}(1-c))))$ $+ \bar{sg}(1 - \max(((ab + \bar{sg}(1-a))b + \bar{sg}(1-b)),$ $(cd + \bar{sg}(1-c))d + \bar{sg}(1-d)))\rangle$
$\vee_{2,112}$	$\langle ab + \bar{sg}(1-a) + cd + \bar{sg}(1-c) - (ab$ $+ \bar{sg}(1-a))(cd + \bar{sg}(1-c)), (ab + \bar{sg}(1-a))^2 + \bar{sg}(-ab$ $+ sg(1-a))(d(cd + \bar{sg}(1-c)) + \bar{sg}(1-d))\rangle$
$\wedge_{2,112}$	$\langle ((ab + \bar{sg}(1-a))((ab + \bar{sg}(1-a))b + \bar{sg}(1-b))$ $+ \bar{sg}(1 - (ab + \bar{sg}(1-a)))(cd + \bar{sg}(1-c))),$ $((ab + \bar{sg}(1-a))b + \bar{sg}(1-b)) + d - ((ab + \bar{sg}(1-a))b$ $+ \bar{sg}(1-b))d)((ab + \bar{sg}(1-a))((ab$ $+ \bar{sg}(1-a))b + \bar{sg}(1-b)) + \bar{sg}(1 - (ab + \bar{sg}(1-a)))(cd$ $+ \bar{sg}(1-c)) + \bar{sg}(1 - ((ab$ $+ \bar{sg}(1-a))b + \bar{sg}(1-b)) - d + ((ab$ $+ \bar{sg}(1-a))b + \bar{sg}(1-b))d))\rangle$
$\vee_{2,113}$	$\langle ab + \bar{sg}(1-a) + cd - (ab + \bar{sg}(1-a))(cd + \bar{sg}(1-c)),$ $((ab + \bar{sg}(1-a))b + \bar{sg}(1-b))(d(cd + \bar{sg}(1-c)) + \bar{sg}(1-d))\rangle$
$\wedge_{2,113}$	$\langle ((ab + \bar{sg}(1-a))((ab + \bar{sg}(1-a))b + \bar{sg}(1-b))$ $+ \bar{sg}(1 - (ab + \bar{sg}(1-a))))((cd + \bar{sg}(1-c))((cd$ $+ \bar{sg}(1-c))d + \bar{sg}(1-d)) + \bar{sg}(1 - (cd + \bar{sg}(1-c)))),$ $((ab + \bar{sg}(1-a))b + \bar{sg}(1-b)) + (cd$ $+ \bar{sg}(1-c))d - ((ab + \bar{sg}(1-a))b + \bar{sg}(1-b))((cd$ $+ \bar{sg}(1-c))d + \bar{sg}(1-d))((ab$ $+ \bar{sg}(1-a))((ab + \bar{sg}(1-a))b + \bar{sg}(1-b)) + \bar{sg}(1 - (ab$ $+ \bar{sg}(1-a))))((cd + \bar{sg}(1-c))((cd$ $+ \bar{sg}(1-c))d + \bar{sg}(1-d)) + \bar{sg}(1 - (cd + \bar{sg}(1-c))))$ $+ \bar{sg}(1 - (((ab + \bar{sg}(1-a))b + \bar{sg}(1-b))$ $+(cd + \bar{sg}(1-c))d - ((ab + \bar{sg}(1-a))b$ $+ \bar{sg}(1-b))((cd + \bar{sg}(1-c))d + \bar{sg}(1-d))))\rangle$

$\vee_{2,114}$	$\langle a + \min(\overline{sg}(a), -c(1-c) + sg(c)),$ $a(1-a) + \min(\overline{sg}(a), c(1-c) + \overline{sg}(c)) \rangle$
$\wedge_{2,114}$	$\langle 1 - a - \min(\overline{sg}(a), sg(1-c) - c(1-c)),$ $(1 - a - \min(\overline{sg}(a), sg(1-c) - c(1-c)))$ $(a + \min(\overline{sg}(a), sg(1-c) - c(1-c)))$ $+ \overline{sg}((1 - a - \min(\overline{sg}(a), sg(1-c) - c(1-c)))) \rangle$
$\vee_{2,115}$	$\langle 1 - \min(1 - a, c(1-c) + \overline{sg}(c)),$ $\min(a(1-a) + \overline{sg}(a), c(1-c) + \overline{sg}(c)) \rangle$
$\wedge_{2,115}$	$\langle \min(1 - a, c(1-c) + \overline{sg}(1-c)),$ $(1 - \min(1 - a, c(1-c) + \overline{sg}(1-c))) \min(1 - a,$ $c(1-c) + \overline{sg}(1-c)) + \overline{sg}(\min(1 - a, c(1-c)$ $+ \overline{sg}(1-c))) \rangle$
$\vee_{2,116}$	$\langle \max(a, (1 - (c(1-c) + \overline{sg}(c)))(c(1-c) + \overline{sg}(c))$ $+ \overline{sg}((c(1-c) + \overline{sg}(c))), \min(a(1-a) + \overline{sg}(a),$ $(c(1-c) + \overline{sg}(c))((-c(1-c) + sg(c))(c(1-c)$ $+ \overline{sg}(c)) + \overline{sg}((c(1-c) + \overline{sg}(c)))$ $+ \overline{sg}(-c(1-c) + sg(c))) \rangle$
$\wedge_{2,116}$	$\langle 1 - \max(a, (1 - c(1-c) - \overline{sg}(1-c))(c(1-c)$ $+ \overline{sg}(1-c)) + \overline{sg}(c(1-c) + \overline{sg}(1-c))),$ $(1 - \max(a, (1 - c(1-c) - \overline{sg}(1-c))(c(1-c)$ $+ \overline{sg}(1-c)) + \overline{sg}(c(1-c) + \overline{sg}(1-c)))$ $. \max(a, (1 - c(1-c) - \overline{sg}(1-c))(c(1-c)$ $+ \overline{sg}(1-c)) + \overline{sg}(c(1-c) + \overline{sg}(1-c)))$ $\overline{sg}(1 - \max(a, (1 - c(1-c) - \overline{sg}(1-c))(c(1-c)$ $+ \overline{sg}(1-c)) + \overline{sg}(c(1-c) + \overline{sg}(1-c))) \rangle$
$\vee_{2,117}$	$\langle a - a(c(1-c) + \overline{sg}(c)),$ $(a(1-a) + \overline{sg}(a))(c(1-c) + \overline{sg}(c)) \rangle$
$\wedge_{2,117}$	$\langle 1 - a + a(c(1-c) + \overline{sg}(1-c)),$ $(1 - a + a(c(1-c) + \overline{sg}(1-c)))(a - a(c(1-c)$ $+ \overline{sg}(1-c)) + \overline{sg}(1 - a + a(c(1-c) + \overline{sg}(1-c))) \rangle$
$\vee_{2,118}$	$\langle a + (-c(1-c) + sg(c))(c(1-c) + \overline{sg}(c))$ $- a((-c(1-c) + sg(c))(c(1-c) + \overline{sg}(c)) + \overline{sg}((c(1-c)$ $+ \overline{sg}(c)))), (a(1-a) + \overline{sg}(a))(c(1-c)$ $+ \overline{sg}(c))((-c(1-c) + sg(c))(c(1-c) + \overline{sg}(c))$ $+ \overline{sg}((c(1-c) + \overline{sg}(c)))) + \overline{sg}(-c(1-c) + sg(c)) \rangle$

	$+sg(b)) + \overline{sg}(b(1 - b) + \overline{sg}(b)) + \overline{sg}((b(1 - b) + \overline{sg}(b))$ $\cdot (b(1 - b) + sg(b)) + \overline{sg}(b(1 - b) + \overline{sg}(b))), (1 - d)$ $\cdot (d(1 - d) + \overline{sg}(1 - d))) + \overline{sg}(d)))$
$\vee_{2,122}$	$\langle b(1 - b) + \overline{sg}(b) + (d(1 - d) + \overline{sg}(d))$ $- (b(1 - b) + \overline{sg}(b))(d(1 - d) + \overline{sg}(d)), ((1 - (d(1 - d)$ $+ \overline{sg}(d)))(b(1 - b) + \overline{sg}(b)) + \overline{sg}(b(1 - b)$ $+ \overline{sg}(b)))(1 - (d(1 - d) + \overline{sg}(d))))\rangle$
$\wedge_{2,122}$	$\langle ((1 - d)(b(1 - b) + \overline{sg}(b))(b(1 - b)$ $+ sg(b)) + \overline{sg}(b(1 - b) + \overline{sg}(b)) + \overline{sg}((b(1 - b)$ $+ \overline{sg}(b))(b(1 - b) + sg(b)) + \overline{sg}(b(1 - b)$ $+ \overline{sg}(b)))(1 - d), (1 - ((1 - d)(b(1 - b) +$ $+ \overline{sg}(b))(b(1 - b) + sg(b)) + \overline{sg}(b(1 - b) + \overline{sg}(b))$ $+ \overline{sg}((b(1 - b) + \overline{sg}(b))(b(1 - b) + sg(b))$ $+ \overline{sg}(b(1 - b) + \overline{sg}(b))))(1 - d)((1 - d)(b(1 - b)$ $+ \overline{sg}(b))(b(1 - b) + sg(b)) + \overline{sg}(b(1 - b) + \overline{sg}(b))$ $+ \overline{sg}((b(1 - b) + \overline{sg}(b))(b(1 - b)$ $+ sg(b)) + \overline{sg}(b(1 - b) + \overline{sg}(b))))(1 - d)$ $+ \overline{sg}(((1 - d)(b(1 - b) + \overline{sg}(b))(b(1 - b)$ $+ sg(b)) + \overline{sg}(b(1 - b) + \overline{sg}(b)) + \overline{sg}((b(1 - b)$ $+ \overline{sg}(b))(b(1 - b) + sg(b)) + \overline{sg}(b(1 - b) + \overline{sg}(b))))(1 - d)\rangle$
$\vee_{2,123}$	$\langle b + (d(1 - d) + \overline{sg}(d))(1 - (d(1 - d) + \overline{sg}(d)))$ $- (b(1 - b) + \overline{sg}(b))((d(1 - d) + \overline{sg}(d))(1$ $- (d(1 - d) + \overline{sg}(d))) - \overline{sg}(1 - (d(1 - d) + \overline{sg}(d)))),$ $((-b(1 - b) + sg(b))(b(1 - b) + \overline{sg}(b)) + \overline{sg}(b(1 - b)$ $+ \overline{sg}(b)))(((1 - (d(1 - d) + \overline{sg}(d)))(d(1 - d)$ $+ \overline{sg}(d))(1 - (d(1 - d) + \overline{sg}(d))) + \overline{sg}(1 - (d(1 - d)$ $+ \overline{sg}(d)))) + \overline{sg}((d(1 - d) + \overline{sg}(d))))\rangle$
$\wedge_{2,123}$	$\langle ((1 - (b(1 - b) + \overline{sg}(b))(b(1 - b) + sg(b))$ $+ \overline{sg}(b(1 - b) + \overline{sg}(b))(b(1 - b) + \overline{sg}(b))(b(1 - b)$ $+ sg(b)) + \overline{sg}(b(1 - b) + \overline{sg}(b)) + \overline{sg}((b(1 - b)$ $+ \overline{sg}(b))(b(1 - b) + sg(b)) + \overline{sg}(b(1 - b)$ $+ \overline{sg}(b)))(((1 - d)(d(1 - d) + \overline{sg}(1 - d)))$ $+ \overline{sg}(d)), (1 - ((1 - (b(1 - b) + \overline{sg}(b))(b(1 - b)$ $+ sg(b)) + \overline{sg}(b(1 - b) + \overline{sg}(b))(b(1 - b)$ $+ \overline{sg}(b))(b(1 - b) + sg(b)) + \overline{sg}(b(1 - b) + \overline{sg}(b))$ $+ \overline{sg}((b(1 - b) + \overline{sg}(b))(b(1 - b) + sg(b))$ $+ \overline{sg}(b(1 - b) + \overline{sg}(b))))(((1 - d)(d(1 - d)$

	$+ \overline{sg}(1 - b))a(ab + \overline{sg}(1 - b) + \overline{sg}(1 - a))$ $+ \overline{sg}(1 - a(ab + \overline{sg}(1 - b) + \overline{sg}(1 - a))))$ $+ \overline{sg}(1 - ((ab + \overline{sg}(1 - b))b + \overline{sg}(1 - b))))\rangle$
$\vee_{2,127}$	$\langle a + c - ac, (cd + \overline{sg}(1 - d))b \rangle$
$\wedge_{2,127}$	$\langle (cd + \overline{sg}(1 - c))a, b + d - bd \rangle$
$\vee_{2,128}$	$\langle c + ab(cd + \overline{sg}(1 - d))(a(ab + \overline{sg}(1 - b))$ $+ \overline{sg}(1 - a)) - c(ab(cd + \overline{sg}(1 - d))(a(ab + \overline{sg}(1 - b))$ $+ \overline{sg}(1 - a)) + \overline{sg}(1 - (cd + \overline{sg}(1 - d))(a(ab + \overline{sg}(1 - b))$ $+ \overline{sg}(1 - a))), (cd + \overline{sg}(1 - d))(ab(ab(cd$ $+ \overline{sg}(1 - d))(a(ab + \overline{sg}(1 - b)) + \overline{sg}(1 - a))$ $+ \overline{sg}(1 - (cd + \overline{sg}(1 - d))(a(ab + \overline{sg}(1 - b))$ $+ \overline{sg}(1 - a))) + \overline{sg}(1 - ab))\rangle$
$\wedge_{2,128}$	$\langle (c + ab(cd + \overline{sg}(1 - d))(a(ab + \overline{sg}(1 - b))$ $+ \overline{sg}(1 - a)) - c(ab(cd + \overline{sg}(1 - d))(a(ab + \overline{sg}(1 - b))$ $+ \overline{sg}(1 - a)) + \overline{sg}(1 - (cd + \overline{sg}(1 - d))(a(ab + \overline{sg}(1 - b))$ $+ \overline{sg}(1 - a))))(cd + \overline{sg}(1 - d))(ab(ab(cd + \overline{sg}(1 - d))$ $.(a(ab + \overline{sg}(1 - b)) + \overline{sg}(1 - a)) + \overline{sg}(1 - (cd$ $+ \overline{sg}(1 - d))(a(ab + \overline{sg}(1 - b)) + \overline{sg}(1 - a))))$ $+ \overline{sg}(1 - ab)), (c + ab(cd + \overline{sg}(1 - d))(a(ab + \overline{sg}(1 - b))$ $+ \overline{sg}(1 - a)) - c(ab(cd + \overline{sg}(1 - d))(a(ab + \overline{sg}(1 - b))$ $+ \overline{sg}(1 - a)) + \overline{sg}(1 - (cd + \overline{sg}(1 - d))(a(ab + \overline{sg}(1 - b))$ $+ \overline{sg}(1 - a))))^2(cd + \overline{sg}(1 - d))(ab(ab(cd + \overline{sg}(1 - d))$ $.(a(ab + \overline{sg}(1 - b)) + \overline{sg}(1 - a)) + \overline{sg}(1 - (cd + \overline{sg}(1 - d))$ $.(a(ab + \overline{sg}(1 - b)) + \overline{sg}(1 - a)))) + \overline{sg}(1 - ab))(c + ab(cd$ $+ \overline{sg}(1 - d))(a(ab + \overline{sg}(1 - b)) + \overline{sg}(1 - a)) - c(ab(cd$ $+ \overline{sg}(1 - d))(a(ab + \overline{sg}(1 - b)) + \overline{sg}(1 - a)) + \overline{sg}(1$ $-(cd + \overline{sg}(1 - d))(a(ab + \overline{sg}(1 - b)) + \overline{sg}(1 - a))))\overline{sg}(1$ $-(cd + \overline{sg}(1 - d))(ab(ab(cd + \overline{sg}(1 - d))(a(ab + \overline{sg}(1 - b))$ $+ \overline{sg}(1 - a)) + \overline{sg}(1 - (cd + \overline{sg}(1 - d))(a(ab$ $+ \overline{sg}(1 - b)) + \overline{sg}(1 - a)))) + \overline{sg}(1 - ab))\rangle$
$\vee_{2,129}$	$\langle c + \min(\overline{sg}(c), a), (1 - c)c + \min(\overline{sg}(c), 1 - a) \rangle$
$\wedge_{2,129}$	$\langle c - \min(\overline{sg}(1 - c), 1 - a), 1 - c + \min(\overline{sg}(1 - c), 1 - a) \rangle$
$\vee_{2,130}$	$\langle 1 - \min(1 - c, 1 - a), \min((1 - c)c + \overline{sg}(c), 1 - a) \rangle$
$\wedge_{2,130}$	$\langle \min(a, c), 1 - \min(c, a) \rangle$
$\vee_{2,131}$	$\langle \max(1 - d, (1 - (a(1 - a) + \overline{sg}(a)))(a(1 - a) + \overline{sg}(a))$ $+ \overline{sg}((a(1 - a) + \overline{sg}(a)))), \min(d(1 - d) + \overline{sg}(1 - d),$ $(a(1 - a) + \overline{sg}(a))((1 - (a(1 - a) + \overline{sg}(a)))(a(1 - a)$

	$+ \overline{sg}(a) + \overline{sg}((a(1-a) + \overline{sg}(a)))$ $+ \overline{sg}(1 - (a(1-a) + \overline{sg}(a))))\rangle$
$\wedge_{2,131}$	$\langle \max(1-c, (1-(a(1-a) + \overline{sg}(a)))(a(1-a) + \overline{sg}(a))$ $+ \overline{sg}((a(1-a) + \overline{sg}(a)))) - \max(1-c, (1-(a(1-a)$ $+ \overline{sg}(a)))(a(1-a) + \overline{sg}(a)) + \overline{sg}((a(1-a) + \overline{sg}(a))))^2$ $+ \overline{sg}(\max(1-c, (1-(a(1-a) + \overline{sg}(a)))(a(1-a)$ $+ \overline{sg}(a)) + \overline{sg}((a(1-a) + \overline{sg}(a))))), \max(1-c, (1$ $- (a(1-a) + \overline{sg}(a)))(a(1-a) + \overline{sg}(a)) + \overline{sg}((a(1-a)$ $+ \overline{sg}(a)))^2 - \max(1-c, (1-(a(1-a) + \overline{sg}(a)))(a(1-a)$ $+ \overline{sg}(a)) + \overline{sg}((a(1-a) + \overline{sg}(a))))^3 + \overline{sg}(1 - \max(1-c,$ $(1-(a(1-a) + \overline{sg}(a)))(a(1-a) + \overline{sg}(a)) + \overline{sg}((a(1-a)$ $+ \overline{sg}(a)))) + a\overline{sg}(\max(1-c, (1-(a(1-a) + \overline{sg}(a)))$. $(a(1-a) + \overline{sg}(a)) + \overline{sg}((a(1-a) + \overline{sg}(a))))\rangle$
$\vee_{2,132}$	$\langle 1 - (1-a)(1-c), ((1-c)c + \overline{sg}(c))(1-a)\rangle$
$\wedge_{2,132}$	$\langle ac, 1-ac\rangle$
$\vee_{2,133}$	$\langle 1-d+a(1-a)(1-a(1-a)) - (1-d)(a(1-a)$. $(1-a(1-a)) + \overline{sg}(a(1-a))), (d(1-d) + \overline{sg}(1-d))$. $((1-a)a(a(1-a)(1-a(1-a)) + \overline{sg}(a(1-a)))$ $+ \overline{sg}(1-a(1-a)))\rangle$
$\wedge_{2,133}$	$\langle 1-c+a(1-a)(1-a(1-a)) - (1-c)(a(1-a)(1-a$. $(1-a)) + \overline{sg}(a(1-a))) - (1-c+a(1-a)(1-a(1-a))$ $-(1-c)(a(1-a)(1-a(1-a)) + \overline{sg}(a(1-a))))^2, (1-c$ $+a(1-a)(1-a(1-a)) - (1-c)(a(1-a)(1-a(1-a))$ $+ \overline{sg}(a(1-a)))^2 - (1-c+a(1-a)(1-a(1-a))$ $-(1-c)(a(1-a)(1-a(1-a)) + \overline{sg}(a(1-a)))^3$ $+(1-c+a(1-a)(1-a(1-a)) - (1-c)(a(1-a)(1-a$. $(1-a)) + \overline{sg}(a(1-a))))\overline{sg}(1-c+a(1-a)(1-a(1-a))$ $-(1-c)(a(1-a)(1-a(1-a)) + \overline{sg}(a(1-a))))$ $+ \overline{sg}(d-a(1-a)(1-a(1-a)) + (1-d)(a(1-a)(1$ - $a(1-a)) + \overline{sg}(a(1-a))))\rangle$
$\vee_{2,134}$	$\langle (1-d) + \min(\overline{sg}((1-d)), 1-b),$ $(d)(1-d) + \min(\overline{sg}((1-d)), (b))\rangle$
$\wedge_{2,134}$	$\langle (1-d)d + \min(\overline{sg}(d), 1-b),$ $1 - (1-d)d - \min(\overline{sg}(d), 1-b)\rangle$
$\vee_{2,135}$	$\langle \max(1-b, 1-d), \min(d(1-d) + \overline{sg}((1-d)), b)\rangle$
$\wedge_{2,135}$	$\langle \min((1-d)d + \overline{sg}(d), 1-b),$ $1 - \min((1-d)d + \overline{sg}(d), 1-b)\rangle$

$\vee_{2,136}$	$\begin{aligned} & \langle \max(c, ((1-b)(b(1-b) + \overline{sg}(1-b)) + \overline{sg}(b))(1 \\ & - ((1-b)(b(1-b) + \overline{sg}(1-b)) + \overline{sg}(b))) + \overline{sg}(1 \\ & - ((1-b)(b(1-b) + \overline{sg}(1-b)) + \overline{sg}(b))), \\ & \min((1-c)c + \overline{sg}(c), (1 - ((1-b)(b(1-b) \\ & + \overline{sg}(1-b)) + \overline{sg}(b)))(((1-b)(b(1-b) \\ & + \overline{sg}(1-b)) + \overline{sg}(b))(1 - ((1-b)(b(1-b) \\ & - b) + \overline{sg}(1-b)) + \overline{sg}(b))) + \overline{sg}(1 - ((1-b)(b(1-b) \\ & + \overline{sg}(1-b)) + \overline{sg}(b)))) + \overline{sg}(((1-b)(b(1-b) \\ & + \overline{sg}(1-b)) + \overline{sg}(b)))) \rangle \end{aligned}$
$\wedge_{2,136}$	$\begin{aligned} & \langle \max(c, ((1-b)(b(1-b) + \overline{sg}(1-b)) + \overline{sg}(b))(1 \\ & - ((1-b)(b(1-b) + \overline{sg}(1-b)) + \overline{sg}(b))) \\ & + \overline{sg}(1 - ((1-b)(b(1-b) + \overline{sg}(1-b)) + \overline{sg}(b)))) \\ & - \max(c, ((1-b)(b(1-b) + \overline{sg}(1-b)) \\ & + \overline{sg}(b))(1 - ((1-b)(b(1-b) \\ & + \overline{sg}(1-b)) + \overline{sg}(b))) + \overline{sg}(1 - ((1-b)(b(1-b) \\ & + \overline{sg}(1-b)) + \overline{sg}(b)))^2 + \overline{sg}(\max(c, \\ & ((1-b)(b(1-b) + \overline{sg}(1-b)) + \overline{sg}(b))(1 \\ & - ((1-b)(b(1-b) + \overline{sg}(1-b)) + \overline{sg}(b))) \\ & + \overline{sg}(1 - ((1-b)(b(1-b) + \overline{sg}(1-b)) \\ & + \overline{sg}(b)))), \max(c, ((1-b)(b(1-b) \\ & + \overline{sg}(1-b)) + \overline{sg}(b))(1 - ((1-b)(b(1-b) \\ & + \overline{sg}(1-b)) + \overline{sg}(b))) + \overline{sg}(1 - ((1-b)(b(1-b) \\ & + \overline{sg}(1-b)) + \overline{sg}(b)))^2 - \max(c, ((1-b)(b(1 \\ & - b) + \overline{sg}(1-b)) + \overline{sg}(b))(1 - ((1-b)(b(1-b) \\ & + \overline{sg}(1-b)) + \overline{sg}(b))) + \overline{sg}(1 - ((1-b)(b(1-b) \\ & + \overline{sg}(1-b)) + \overline{sg}(b)))^3 + \overline{sg}(1 - \max(c, \\ & ((1-b)(b(1-b) + \overline{sg}(1-b)) + \overline{sg}(b))(1 \\ & - ((1-b)(b(1-b) + \overline{sg}(1-b)) + \overline{sg}(b))) \\ & + \overline{sg}(1 - ((1-b)(b(1-b) + \overline{sg}(1-b)) + \overline{sg}(b)))))) \rangle \end{aligned}$
$\vee_{2,137}$	$\langle 1 - b + b(1-d), (d(1-d) + \overline{sg}((1-d)))b \rangle$
$\wedge_{2,137}$	$\langle ((1-d)d + \overline{sg}(d))(1-b), 1 - ((1-d)d + \overline{sg}(d))(1-b) \rangle$
$\vee_{2,138}$	$\begin{aligned} & \langle c + ((1-b)(b(1-b) + \overline{sg}(1-b)) + \overline{sg}(b))(1 - ((1-b) \\ & .(b(1-b) + \overline{sg}(1-b)) + \overline{sg}(b))) - c(((1-b)(b(1-b) \\ & + \overline{sg}(1-b)) + \overline{sg}(b))(1 - ((1-b)(b(1-b) + \overline{sg}(1-b)) \\ & + \overline{sg}(b))) + \overline{sg}(1 - ((1-b)(b(1-b) + \overline{sg}(1-b)) + \overline{sg}(b)))), \\ & ((1-c)c + \overline{sg}(c))((1 - ((1-b)(b(1-b) + \overline{sg}(1-b)) \\ & + \overline{sg}(b)))((1-b)(b(1-b) + \overline{sg}(1-b)) + \overline{sg}(b))(1 \end{aligned}$

	$ +\overline{sg}(1-b)) + \overline{sg}(b)))))) \rangle$
$\vee_{2,139}$	$\langle \frac{3+2a+c}{8}, \frac{2+2b+d}{8} \rangle$
$\wedge_{2,139}$	$\langle \frac{3+a+2c}{16}, \frac{10+b+2d}{16} \rangle$
$\vee_{2,140}$	$\langle \frac{3a+2c+10}{27}, \frac{3b+2d+12}{27} \rangle$
$\wedge_{2,140}$	$\langle \frac{a+14+6c}{81}, \frac{b+6d+60}{81} \rangle$
$\vee_{2,141}$	$\langle \frac{6a+4c+5+\max(6a+3,4c+2)}{27}, \frac{6b+4d+3+\min(6b,4d+3)}{27} \rangle$
$\wedge_{2,141}$	$\langle \frac{8a+12c+10+2\min(4a+2,6c+3)}{81}, \frac{16b+24d+14+4\max(4b+3,6d)}{81} \rangle$
$\vee_{2,142}$	$\langle 1 - \frac{10-3a-c+\max(3-3a,7-c)}{27}, \frac{10-3a-c+\max(3-3a,7-c)}{27} \rangle$
$\wedge_{2,142}$	$\langle \frac{a+3c+8+\max(2+a,6+3c)}{81}, 1 - \frac{a+3c+8+\max(2+a,6+3c)}{81} \rangle$
$\vee_{2,143}$	$\langle 1 - \frac{10-3a-c+\max(3-3a,7-c)}{27}, \frac{10-3a-c+\max(3-3a,7-c)}{27} \rangle$
$\wedge_{2,143}$	$\langle \frac{5+a-3c+\max(2+a,3-3c)}{81}, 1 - \frac{5+a-3c+\max(2+a,3-3c)}{81} \rangle$
$\vee_{2,144}$	$\langle \frac{15-3b-2d}{27}, 1 - \frac{15-3b-2d}{27} \rangle$
$\wedge_{2,144}$	$\langle \frac{21-b-6d}{81}, 1 - \frac{21-b-6d}{81} \rangle$
$\vee_{2,145}$	$\langle \frac{15-3b-2d}{27}, 1 - \frac{15-3b-2d}{27} \rangle$
$\wedge_{2,145}$	$\langle \frac{21-b-6d}{81}, 1 - \frac{21-b-6d}{81} \rangle$
$\vee_{2,146}$	$\langle \frac{6a+4c+14-\min(6-6a,7-4c)}{27}, 1 - \frac{6a+4c+14-\min(6-6a,7-4c)}{27} \rangle$
$\wedge_{2,146}$	$\langle \frac{8a+12c+10+2\min(4a+2,6c+3)}{81},$ $1 - \frac{8a+12c+10+2\min(4a+2,6c+3)}{81} \rangle$
$\vee_{2,147}$	$\langle \frac{6a+4c+5+\max(6a+3,4c+2)}{27}, 1 - \frac{6a+4c+5+\max(6a+3,4c+2)}{27} \rangle$
$\wedge_{2,147}$	$\langle \frac{4a+6c+28-2\max(7-4a,6-6c)}{81}, 1 - \frac{4a+6c+28-2\max(7-4a,6-6c)}{81} \rangle$
$\vee_{2,148}$	$\langle \frac{24-12b-8d-2\max(9-6b,6-4d)}{27},$ $1 - \frac{24-12b-8d-2\max(9-6b,6-4d)}{27} \rangle$
$\wedge_{2,148}$	$\langle \frac{48-8b-4d-\max(3+4d,6d)}{81}, 1 - \frac{48-8b-4d-\max(3+4d,6d)}{81} \rangle$
$\vee_{2,149}$	$\langle \frac{15-6b-4d+\max(9-6b,6-4d)}{27}, 1 - \frac{15-6b-4d+\max(9-6b,6-4d)}{27} \rangle$
$\wedge_{2,149}$	$\langle \frac{48-8b-12d-2\max(3+4b,6d)}{81}, 1 - \frac{48-8b-12d-2\max(3+4b,6d)}{81} \rangle$
$\vee_{2,150}$	$\langle \frac{2\lambda.a+c+4\lambda^3-\lambda}{8\lambda^3}, \frac{2\lambda.b+d+4\lambda^3-\lambda-1}{8\lambda^3} \rangle$
$\wedge_{2,150}$	$\langle \frac{a+2\lambda.c+4\lambda^2-\lambda+2\lambda(2\lambda-1)(\lambda-1)}{16\lambda^4}, \frac{b+2\lambda.d+4\lambda^3+4\lambda^2-\lambda-1}{16\lambda^4} \rangle$
$\vee_{2,151}$	$\langle \frac{(a+\gamma)(2\gamma+1)+c+2\gamma^2+2\gamma+\gamma(2\gamma+1)^2}{(2\gamma+1)^3},$ $\frac{(b+\gamma)(2\gamma+1)+d+2\gamma^2+2\gamma+(\gamma-1)(2\gamma+1)^2}{(2\gamma+1)^3} \rangle$
$\wedge_{2,151}$	$\langle \frac{a+(2\gamma+1)c+4\gamma^2+3\gamma+(2\gamma^2+2\gamma-1)(2\gamma+1)^2}{(2\gamma+1)^4},$ $\frac{b+(2\gamma+1)d+(2\gamma^2+2\gamma)(4\gamma^2+4\gamma+2)}{(2\gamma+1)^4} \rangle$
$\vee_{2,152}$	$\langle \frac{(a+\beta)(\alpha+\beta)+c+\alpha^2+\alpha\beta+(\alpha+\beta)^2(\alpha-1)}{(\alpha+\beta)^3},$

	$\frac{(b+\alpha-1)(\alpha+\beta)+d+\alpha-1+\beta(\alpha+\beta)+(\alpha+\beta)^2(\beta-1)}{(\alpha+\beta)^3}$
$\wedge_{2,152}$	$\langle \frac{(\alpha-1)(\alpha+\beta)^3+a+(\alpha-1)(\alpha+\beta)+\beta+(\beta-1)(\alpha+\beta)^2+(c+\beta)(\alpha+\beta)}{(\alpha+\beta)^4},$ $\frac{\beta(\alpha+\beta)^3+b+\alpha-1+\beta(\alpha+\beta)+(\alpha-1)(\alpha+\beta)^2+(d+\alpha-1)(\alpha+\beta)}{(\alpha+\beta)^4} \rangle$
$\vee_{2,153}$	$\langle \min(1, \max(c, \max(0, a - \eta) + \varepsilon)),$ $\max(0, \min(d, \min(1, b + \varepsilon) - \eta)) \rangle$
$\wedge_{2,153}$	$\langle \min(1, \max(0, \min(\max(0, c - \eta),$ $\min(1, \max(0, a - \eta) + \varepsilon) - \eta)) + \varepsilon),$ $\max(0, \min(1, \max(\min(1, d + \varepsilon),$ $\max(0, \min(1, b + \varepsilon) - \eta) + \varepsilon)) - \eta) \rangle$
$\vee_{2,154}$	$\langle \frac{4\lambda^3+(2a-1)\lambda+c}{8\lambda^3}, \frac{4\lambda^3+(1-2c)\lambda-a}{8\lambda^3} \rangle$
$\wedge_{2,154}$	$\langle \frac{1}{2} - \frac{4\lambda^3+(1-2c)\lambda-a}{16\lambda^4}, \frac{1}{2} + \frac{4\lambda^3+(1-2c)\lambda-a}{16\lambda^4} \rangle$
$\vee_{2,155}$	$\langle 1 - \frac{4\lambda^3-(1-2a)\lambda-c}{8\lambda^3}, \frac{4\lambda^3-(1-2a)\lambda-c}{8\lambda^3} \rangle$
$\wedge_{2,155}$	$\langle \frac{1}{2} - \frac{4\lambda^3+(1-2b)\lambda-a}{16\lambda^4}, \frac{1}{2} + \frac{4\lambda^3+(1-2b)\lambda-a}{16\lambda^4} \rangle$
$\vee_{2,156}$	$\langle \frac{4\lambda^3+(5-2b)\lambda+1-d}{8\lambda^3}, 1 - \frac{4\lambda^3+(5-2b)\lambda+1-d}{8\lambda^3} \rangle$
$\wedge_{2,156}$	$\langle \frac{8\lambda^4-4\lambda^3+(1-2d)\lambda+1-b}{16\lambda^4}, 1 - \frac{8\lambda^4-4\lambda^3+(1-2d)\lambda+1-b}{16\lambda^4} \rangle$
$\vee_{2,157}$	$\langle \frac{4\lambda^3+(1-2b)\lambda+1-d}{8\lambda^3}, 1 - \frac{4\lambda^3+(1-2b)\lambda+1-d}{8\lambda^3} \rangle$
$\wedge_{2,157}$	$\langle \frac{4\lambda^3-2\lambda^2+(2d-1)\lambda+b-1}{8\lambda^3}, 1 - \frac{4\lambda^3-2\lambda^2+(2d-1)\lambda+b-1}{8\lambda^3} \rangle$
$\vee_{2,158}$	$\langle 1 - \frac{\gamma(2\gamma+1)^2+(1-a+\gamma)(2\gamma+1)-2\gamma^2-2\gamma-c}{(2\gamma+1)^3},$ $\gamma(2\gamma+1)^2+(1-a+\gamma)(2\gamma+1)-2\gamma^2-2\gamma-c \rangle$
$\wedge_{2,158}$	$\langle 1 - \frac{\gamma(2\gamma+1)^3+(1+\gamma)(2\gamma+1)^2-c(2\gamma+1)+1-\alpha+\gamma}{(2\gamma+1)^4},$ $\gamma(2\gamma+1)^3+(1+\gamma)(2\gamma+1)^2-c(2\gamma+1)+1-\alpha+\gamma \rangle$
$\vee_{2,159}$	$\langle 1 - \frac{(\gamma-1)(2\gamma+1)^2+(1-a+\gamma)(2\gamma+1)+2\gamma^2+2\gamma+1-c}{(2\gamma+1)^3},$ $(\gamma-1)(2\gamma+1)^2+(1-a+\gamma)(2\gamma+1)+2\gamma^2+2\gamma+1-c \rangle$
$\wedge_{2,159}$	$\langle 1 - \frac{\gamma(2\gamma+1)^3+(1+\gamma)(2\gamma+1)^2-c(2\gamma+1)+1-\alpha+\gamma}{(2\gamma+1)^4},$ $\gamma(2\gamma+1)^3+(1+\gamma)(2\gamma+1)^2-c(2\gamma+1)+1-\alpha+\gamma \rangle$
$\vee_{2,160}$	$\langle \frac{(\gamma+1)(2\gamma+1)^2+(1-b+\gamma)(2\gamma+1)-2\gamma^2-2\gamma-d}{(2\gamma+1)^3},$ $1 - \frac{(\gamma+1)(2\gamma+1)^2+(1-b+\gamma)(2\gamma+1)-2\gamma^2-2\gamma-d}{(2\gamma+1)^3} \rangle$
$\wedge_{2,160}$	$\langle \frac{\gamma(2\gamma+1)^3+\gamma(2\gamma+1)^2-d(2\gamma+1)+1-\beta+\gamma}{(2\gamma+1)^4},$ $1 - \frac{\gamma(2\gamma+1)^3+\gamma(2\gamma+1)^2-d(2\gamma+1)+1-\beta+\gamma}{(2\gamma+1)^4} \rangle$
$\vee_{2,161}$	$\langle \frac{\gamma(2\gamma+1)^2+(1-b+\gamma)(2\gamma+1)+2\gamma^2+2\gamma+1-d}{(2\gamma+1)^3},$

	$1 - \frac{\gamma(2\gamma+1)^2 + (1-b+\gamma)(2\gamma+1) + 2\gamma^2 + 2\gamma + 1 - d}{(2\gamma+1)^3}$
$\wedge_{2,161}$	$\langle \frac{\gamma(2\gamma+1)^3 + \gamma(2\gamma+1)^2 - d(2\gamma+1) + 1 - \beta + \gamma}{(2\gamma+1)^4},$ $1 - \frac{\gamma(2\gamma+1)^3 + \gamma(2\gamma+1)^2 - d(2\gamma+1) + 1 - \beta + \gamma}{(2\gamma+1)^4} \rangle$
$\vee_{2,162}$	$\langle 1 - \frac{(b-1+\alpha)(\alpha+\beta) - d - \alpha^2 + \beta(\alpha+\beta)^2 - \alpha\beta}{(\alpha+\beta)^3},$ $\frac{(b-1+\alpha)(\alpha+\beta) - d - \alpha^2 + \beta(\alpha+\beta)^2 - \alpha\beta}{(\alpha+\beta)^3} \rangle$
$\wedge_{2,162}$	$\langle \frac{(\alpha-1)(\alpha+\beta)^2 + \beta(\alpha+\beta) + 1 - d}{(\alpha+\beta)^3},$ $\frac{\beta(\alpha+\beta)^2 + \beta(\alpha+\beta) + 1 - d}{(\alpha+\beta)^3} \rangle$
$\vee_{2,163}$	$\langle \frac{\alpha(\alpha+\beta)^2 - (b-1)(\alpha+\beta) - d - \alpha + 1}{(\alpha+\beta)^3},$ $1 - \frac{\alpha(\alpha+\beta)^2 - (b-1)(\alpha+\beta) - d - \alpha + 1}{(\alpha+\beta)^3} \rangle$
$\wedge_{2,163}$	$\langle \frac{(\alpha-1)(\alpha+\beta)^2 + \beta(\alpha+\beta) + c}{(\alpha+\beta)^3},$ $\frac{\beta(\alpha+\beta)^2 + \beta(\alpha+\beta) + c}{(\alpha+\beta)^3} \rangle$
$\vee_{2,164}$	$\langle \frac{\alpha(\alpha+\beta)^2 + (1-b)(\alpha+\beta) - \alpha - d}{(\alpha+\beta)^3},$ $1 - \frac{\alpha(\alpha+\beta)^2 + (1-b)(\alpha+\beta) - \alpha - d}{(\alpha+\beta)^3} \rangle$
$\wedge_{2,164}$	$\langle \frac{(\alpha-1)(\alpha+\beta)^3 + \beta(\alpha+\beta)^2 - d(\alpha+\beta) + 1 - b + \beta}{(\alpha+\beta)^4},$ $1 - \frac{(\alpha-1)(\alpha+\beta)^3 + \beta(\alpha+\beta)^2 - d(\alpha+\beta) + 1 - b + \beta}{(\alpha+\beta)^4} \rangle$
$\vee_{2,165}$	$\langle \frac{(\alpha-1)(\alpha+\beta)^2 + (1-b+2\beta)(\alpha+\beta) - \alpha + 1 - d}{(\alpha+\beta)^3},$ $1 - \frac{(\alpha-1)(\alpha+\beta)^2 + (1-b+2\beta)(\alpha+\beta) - \alpha + 1 - d}{(\alpha+\beta)^3} \rangle$
$\wedge_{2,165}$	$\langle \frac{(\alpha-1)(\alpha+\beta)^3 + \beta(\alpha+\beta)^2 - d(\alpha+\beta) + 1 - b + \beta}{(\alpha+\beta)^4},$ $1 - \frac{(\alpha-1)(\alpha+\beta)^3 + \beta(\alpha+\beta)^2 - d(\alpha+\beta) + 1 - b + \beta}{(\alpha+\beta)^4} \rangle$
$\vee_{2,166}$	$\langle \max(a, \min(b, c)), \min(b, \max(a, d)) \rangle$
$\wedge_{2,166}$	$\langle \min(a, \max(b, c)), \max(b, \min(a, d)) \rangle$
$\vee_{2,167}$	$\langle \max(a, \min(1-a, c)),$ $\min(1-a, 1-\min(1-a, c)) \rangle$
$\wedge_{2,167}$	$\langle 1 - \max(1-a, \min(a, 1-c)),$ $\max(1-a, \min(a, 1-c)) \rangle$
$\vee_{2,168}$	$\langle \max(a, \min(1-a, c)),$ $1 - \max(a, \min(1-a, c)) \rangle$
$\wedge_{2,168}$	$\langle 1 - \max(1-a, \min(a, 1-c)),$ $\max(1-a, \min(a, 1-c)) \rangle$
$\vee_{2,169}$	$\langle \max(1-b, \min(b, (1-d))),$

	$1 - \max(1 - b, \min(b, (1 - d)))\rangle$
$\wedge_{2,169}$	$\langle 1 - \max(b, \min(1 - b, d)),$ $\max(b, \min(1 - b, d))\rangle$
$\vee_{2,170}$	$\langle \max(1 - b, \min(b, d)), 1 - \max(1 - b, \min(b, d))\rangle$
$\wedge_{2,170}$	$\langle 1 - \max(b, \min(1 - b, d)), \max(b, \min(1 - b, d))\rangle$
$\vee_{2,171}$	$\langle \overline{sg}(\max(\overline{sg}(1 - b), sg(d)) - \max(sg(1 - b), \overline{sg}(d))),$ $sg(\max(\overline{sg}(1 - b), sg(d)) - \max(sg(1 - b), \overline{sg}(d)))\rangle$
$\wedge_{2,171}$	$\langle sg(\max(sg(1 - b), sg(1 - d))$ $- \max(\overline{sg}(1 - b), \overline{sg}(1 - d))), \overline{sg}(\max(sg(1 - b),$ $sg(1 - d)) - \max(\overline{sg}(1 - b), \overline{sg}(1 - d)))\rangle$
$\vee_{2,172}$	$\langle \overline{sg}(\overline{sg}(a) - sg(c)), sg(\overline{sg}(a) - sg(c))\rangle$
$\wedge_{2,172}$	$\langle sg(sg(a) - \overline{sg}(c)), \overline{sg}(sg(a) - \overline{sg}(c))\rangle$
$\vee_{2,173}$	$\langle \overline{sg}(\overline{sg}(a) + \overline{sg}(c) - 1), sg(\overline{sg}(a) + \overline{sg}(c) - 1)\rangle$
$\wedge_{2,173}$	$\langle sg(sg(a) + sg(d) - 1), \overline{sg}(sg(a) + sg(d) - 1)\rangle$
$\vee_{2,174}$	$\langle \overline{sg}(sg(1 - b) - \overline{sg}(d)), sg(sg(1 - b) - \overline{sg}(d))\rangle$
$\wedge_{2,174}$	$\langle sg(\overline{sg}(1 - b) - os(1 - d)), \overline{sg}(\overline{sg}(1 - b) - os(1 - d))\rangle$
$\vee_{2,175}$	$\langle \overline{sg}(sg(d) - sg(1 - b)), sg(sg(d) - sg(1 - b))\rangle$
$\wedge_{2,175}$	$\langle sg(sg(1 - d) - \overline{sg}(1 - b)), \overline{sg}(sg(1 - d) - \overline{sg}(1 - b))\rangle$
$\vee_{2,176}$	$\langle \overline{sg}(\overline{sg}(a) + sg(a)b - c) + sg(\overline{sg}(a)$ $+ sg(a)b - c) \max(a, c), sg(\overline{sg}(a) + sg(a)b$ $- c) \min(\overline{sg}(a) + sg(a)b, d)\rangle$
$\wedge_{2,176}$	$\langle \overline{sg}(\overline{sg}(\overline{sg}(\overline{sg}(a) + bsg(a)) + bsg(\overline{sg}(a)$ $+ bsg(a)) - \overline{sg}(c) - dsg(c)) + sg(\overline{sg}(\overline{sg}(a) + bsg(a))$ $+ bsg(\overline{sg}(a) + bsg(a)) - \overline{sg}(c) - dsg(c)) \max(\overline{sg}(a)$ $+ bsg(a), \overline{sg}(c) + dsg(c))) + sg(\overline{sg}(\overline{sg}(\overline{sg}(a)$ $+ bsg(a)) + bsg(\overline{sg}(a) + bsg(a)) - \overline{sg}(c) - dsg(c))$ $+ sg(\overline{sg}(\overline{sg}(a) + bsg(a)) + bsg(\overline{sg}(a) + bsg(a))$ $- \overline{sg}(c) - dsg(c)) \max(\overline{sg}(a) + bsg(a), \overline{sg}(c)$ $+ dsg(c))(sg(\overline{sg}(\overline{sg}(a) + bsg(a)) + bsg(\overline{sg}(a)$ $+ bsg(a)) - \overline{sg}(c) - dsg(c)) \min(\overline{sg}(\overline{sg}(a)$ $+ bsg(a)) + bsg(\overline{sg}(a) + bsg(a)), c)),$ $\overline{sg}(\overline{sg}(\overline{sg}(a) + bsg(a)) + bsg(\overline{sg}(a)$ $+ bsg(a)) - \overline{sg}(c) - dsg(c)) + sg(\overline{sg}(\overline{sg}(a)$ $+ bsg(a)) + bsg(\overline{sg}(a) + bsg(a)) - \overline{sg}(c)$ $- dsg(c)) \max(\overline{sg}(a) + bsg(a), \overline{sg}(c) + dsg(c))\rangle$
$\vee_{2,177}$	$\langle \overline{sg}(\overline{sg}(a) + sg(a)(1 - a) - c) + sg(\overline{sg}(a)$ $+ sg(a)(1 - a) - c) \max(sg(a)(2 - a), c), sg(\overline{sg}(a)$

	$+sg(a)(1-a) - c \min(\overline{sg}(a) + sg(a)(1-a), 1-c) \rangle$
$\wedge_{2,177}$	$\langle \overline{sg}(\overline{sg}(-sg(1-asg(a)) + asg(a - a^2sg(a)) + csg(c)))$ $+sg(-sg(1-asg(a)) + asg(a - a^2sg(a))$ $+csg(c)) \max(sg(1-asg(a)) - asg(a - a^2sg(a)),$ $1 - csg(c)) + sg(\overline{sg}(-sg(1-asg(a)) + asg(a$ $-a^2sg(a)) + csg(c)) + sg(-sg(1-asg(a))$ $+asg(a - a^2sg(a)) + csg(c)) \max(sg(1-asg(a))$ $-asg(a - a^2sg(a)), 1 - csg(c))(sg($ $-sg(1-asg(a)) + asg(a - a^2sg(a))$ $+csg(c)) - sg(-sg(1-asg(a)) + asg(a - a^2sg(a))$ $+csg(c)) \max(sg(1-asg(a)) - asg(a - a^2sg(a)),$ $1 - csg(c)), \overline{sg}(-sg(1-asg(a)) + asg(a$ $-a^2sg(a)) + csg(c)) + sg(-sg(1-asg(a)) + asg(a$ $-a^2sg(a)) + csg(c)) \max(sg(1-asg(a))$ $-asg(a - a^2sg(a)), 1 - csg(c)) \rangle$
$\vee_{2,178}$	$\langle \overline{sg}(-asg(a) + d) + sg(a - 1 + d)(1 - \min(\overline{sg}(a)$ $+sg(a)(1-a), d)), sg(-asg(a) + d) \min(\overline{sg}(a)$ $+sg(a)(1-a), d) \rangle$
$\wedge_{2,178}$	$\langle sg(\overline{sg}(\overline{sg}(1-asg(a)) + asg(a - a^2sg(a)) - 1 + c)$ $+sg(\overline{sg}(1-asg(a)) + asg(a - a^2sg(a)) - 1 + c)(1$ $- \min(\overline{sg}(1-asg(a)) + asg(a - a^2sg(a)), c))$ $+sg(\overline{sg}(\overline{sg}(1-asg(a)) + asg(a - a^2sg(a)) - 1 + c)$ $+sg(\overline{sg}(1-asg(a)) + asg(a - a^2sg(a)) - 1 + c)(1$ $- \min(\overline{sg}(1-asg(a)) + asg(a - a^2sg(a)),$ $c))(sg(\overline{sg}(1-asg(a)) + asg(a - a^2sg(a)) - 1 + c)$ $-sg(\overline{sg}(1-asg(a)) + asg(a - a^2sg(a)) - 1 + c)(1$ $- \min(\overline{sg}(1-asg(a)) + asg(a - a^2sg(a)), c)),$ $\overline{sg}(\overline{sg}(1-asg(a)) + asg(a - a^2sg(a)) - 1 + c)$ $+sg(\overline{sg}(1-asg(a)) + asg(a - a^2sg(a)) - 1 + c)(1$ $- \min(\overline{sg}(1-asg(a)) + asg(a - a^2sg(a)), c)) \rangle$
$\vee_{2,179}$	$\langle \overline{sg}(a - \overline{sg}(c) - (1-c)sg(c)) + sg(a - \overline{sg}(c)$ $+ (1-c)sg(c)) \max(1-a, \overline{sg}(c) + (1-c)sg(c)), sg(a$ $- \overline{sg}(c) - (1-c)sg(c))(1 - \max(1-a, \overline{sg}(c)$ $+ (1-c)sg(c))) \rangle$
$\wedge_{2,179}$	$\langle \overline{sg}(1 - sg(1 - (1-b)sg(1-b) - \overline{sg}(1-d) - dsg(1-d))$ $.(1 - \max((1-b)sg(1-b), \overline{sg}(1-d) + dsg(1-d)))$ $+sg(1 - sg(1 - (1-b)sg(1-b) - \overline{sg}(1-d)$

	$\begin{aligned} & -dsg(1-d)(1 - \max((1-b)sg(1-b), \bar{sg}(1-d)) \\ & + dsg(1-d)))sg(1 - (1-b)sg(1-b) - \bar{sg}(1-d) \\ & - dsg(1-d)(1 - \max((1-b)sg(1-b), \bar{sg}(1-d)) \\ & + dsg(1-d)), 1 - (\bar{sg}(1 - (1-b)sg(1-b) - \bar{sg}(1-d)) \\ & - dsg(1-d)) + sg(1 - (1-b)sg(1-b) - \bar{sg}(1-d) \\ & - dsg(1-d)) \max((1-b)sg(1-b), \bar{sg}(1-d)) \\ & + dsg(1-d))) \end{aligned}$
$\vee_{2,180}$	$\langle \bar{sg}(d-1+a) + sg(d-1+a) \max(1-a, 1-d),$ $sg(d-1+a) \min(a, d) \rangle$
$\vee_{2,181}$	$\langle 1 - \bar{sg}(a). \bar{sg}(c), \bar{sg}(c). \bar{sg}(a) \rangle$
$\wedge_{2,181}$	$\langle \bar{sg}(1 - sg(a)sg(c)), sg(1 - sg(a)sg(c)) \rangle$
$\vee_{2,182}$	$\langle 1 - \bar{sg}(a). \bar{sg}(c), \bar{sg}(c). \bar{sg}(a) \rangle$
$\wedge_{2,182}$	$\langle \bar{sg}(1 - sg(a)sg(c)), sg(1 - sg(a)sg(c)) \rangle$
$\vee_{2,183}$	$\langle 1 - \bar{sg}(a). \bar{sg}(c), \bar{sg}(c). \bar{sg}(a) \rangle$
$\wedge_{2,183}$	$\langle \bar{sg}(1 - sg(a).sg(c)), sg(1 - sg(a).sg(c)) \rangle$
$\vee_{2,184}$	$\langle 1 - \bar{sg}(1-b). \bar{sg}(1-d), \bar{sg}(1-b). \bar{sg}(1-d) \rangle$
$\wedge_{2,184}$	$\langle \bar{sg}(sg(1-d).sg(1-b)), sg(sg(1-d).sg(1-b)) \rangle$
$\vee_{2,185}$	$\langle 1 - \bar{sg}(1-b)\bar{sg}(1-d), (1 - \bar{sg}(d)).\bar{sg}(1-b) \rangle$
$\wedge_{2,185}$	$\langle \bar{sg}(1 - sg(1-d).sg(1-b)), sg(1 - sg(1-d).sg(1-b)) \rangle$

References

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